

Explanatoriness is evidentially irrelevant, or
inference to the best explanation meets
Bayesian
confirmation theory

William Roche and Elliott Sober

(E) If H and O were true, H would explain O

Is E evidence for H ?

According to Bayesian confirmation theory, if E is evidence for H , then:

(E) If H and O were true, H would explain O

Is E evidence for H ?

According to Bayesian confirmation theory, if E is evidence for H , then:

$\Pr(H|E) > \Pr(H)$ **Not plausible unless we know O is true**

(E) If H and O were true, H would explain O

Is E evidence for H ?

According to Bayesian confirmation theory, if E is evidence for H , then:

$\Pr(H|O\&E) > \Pr(H)$ **Doesn't imply that E is evidentially relevant**

(E) If H and O were true, H would explain O

Is E evidence for H ?

According to Bayesian confirmation theory, if E is evidence for H , then:

$\Pr(H|O\&E) > \Pr(H|O)$ This is the correct formulation

(E) If H and O were true, H would explain O

Is E evidence for H ?

According to Bayesian confirmation theory, if E is evidence for H , then:

$\Pr(H|O\&E) > \Pr(H|O)$ Roche and Sober argue this inequality is FALSE

Instead, they argue

$\Pr(H|O\&E) = \Pr(H|O)$ i.e. O screens off E from H

The explanitoriness of H is evidentially idle, given O

E is **not** evidence for H

Example: smoking and lung cancer

Suppose frequency data show a **correlation** between smoking and lung cancer

$$\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50}) = c$$

If the fact that smoking *explains* lung cancer were evidentially relevant, then

$$\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50} \ \& \ \text{if } S \text{ smoked at least 10,000 cigarettes before age 50 and } S \text{ got lung cancer subsequently, then the smoking would explain the lung cancer}) > c$$

Example: smoking and lung cancer

Suppose frequency data show a **correlation** between smoking and lung cancer

Supported by
frequency data

→ $\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50}) = c$

If the fact that smoking *explains* lung cancer were evidentially relevant, then

Not supported
by frequency
data

→ $\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50 \& if S smoked at least 10,000 cigarettes before age 50 and S got lung cancer subsequently, then the smoking would explain the lung cancer}) > c$

FALSE

Example: smoking and lung cancer

Suppose frequency data show a **correlation** between smoking and lung cancer

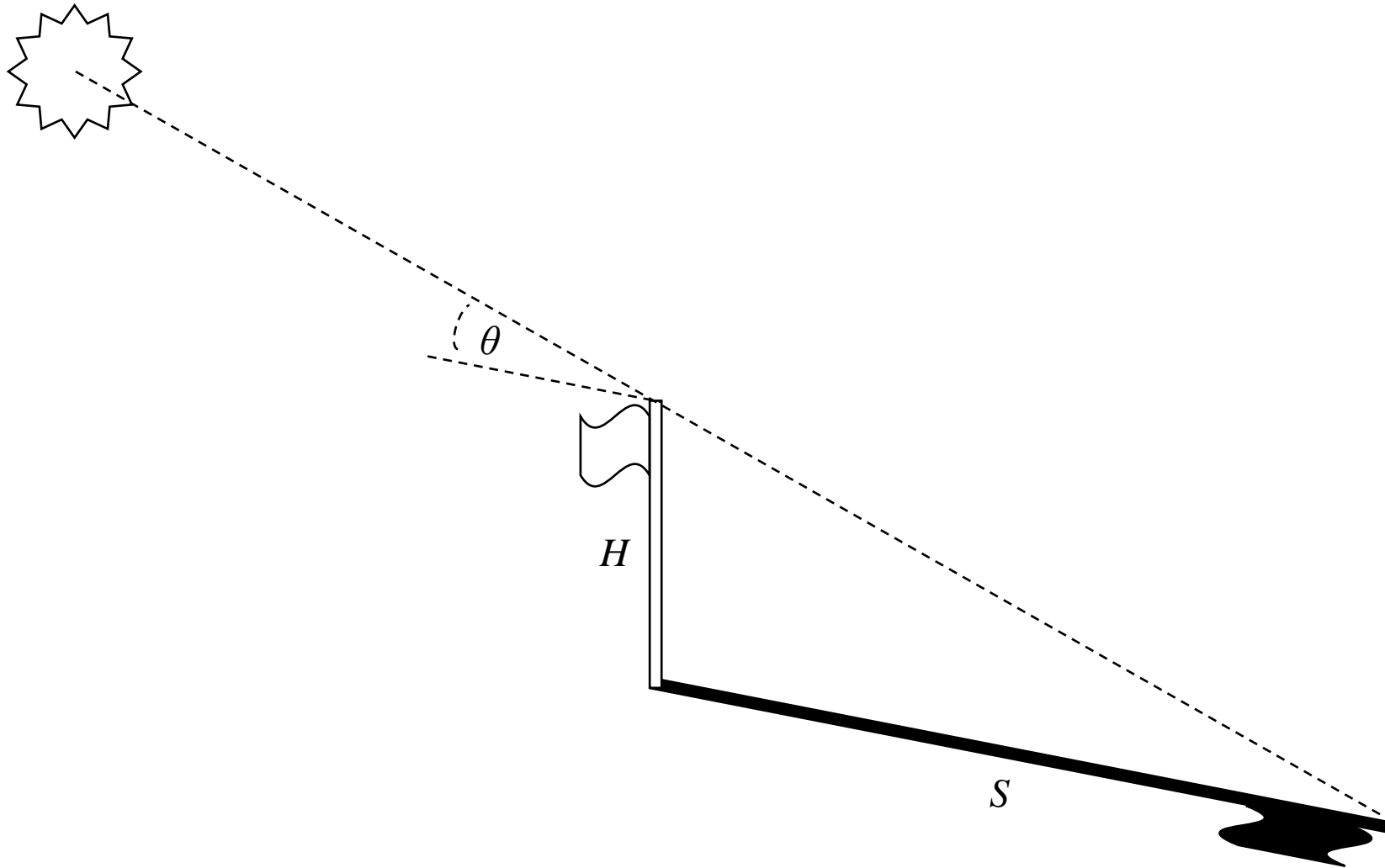
Supported by frequency data → $\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50}) = c$

If the fact that smoking *explains* lung cancer were evidentially relevant, then

Supported by frequency data → $\Pr(S \text{ smoked at least 10,000 cigarettes before age 50} \mid S \text{ got lung cancer after age 50 \& if S smoked at least 10,000 cigarettes before age 50 and S got lung cancer subsequently, then the smoking would explain the lung cancer}) = c$
TRUE

The example assumes a causal notion of explanation: if smoking causes cancer, then smoking *explains* cancer.

As we all know, causation—and hence, causal explanation—is *asymmetric*.



The example assumes a causal notion of explanation: if smoking causes cancer, then smoking *explains* cancer.

As we all know, causation—and hence, causal explanation—is *asymmetric*.

But [Bayesian] confirmation is *symmetric*

$\Pr(Y|X) > \Pr(Y)$ if and only if $\Pr(X|Y) > \Pr(X)$

Hence, it is no surprise that the Bayesian confirmation relation is indifferent to the explanatory relation.

DN explanation fares no better:

Knowing that H entails O —and so explains O , on the DN model—gives us information about confirmation.

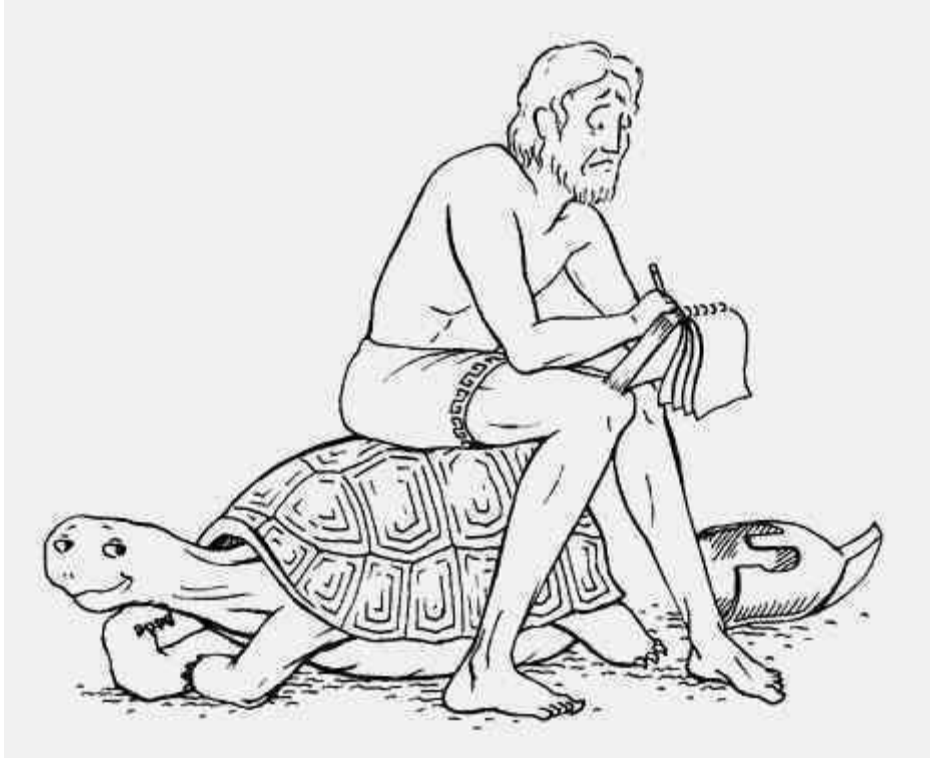
But it is the entailment relationship that does the work, and entailment relationships are already “baked into” the probabilities.

If E is the proposition that H entails O , then

$$\Pr(H|O\&E) = \Pr(H|O) \quad \textit{Screening off still holds}$$

If I is the proposition that O entails H , then

$$\Pr(H|O\&I) = \Pr(H|O) \quad \textit{Screening off still holds}$$

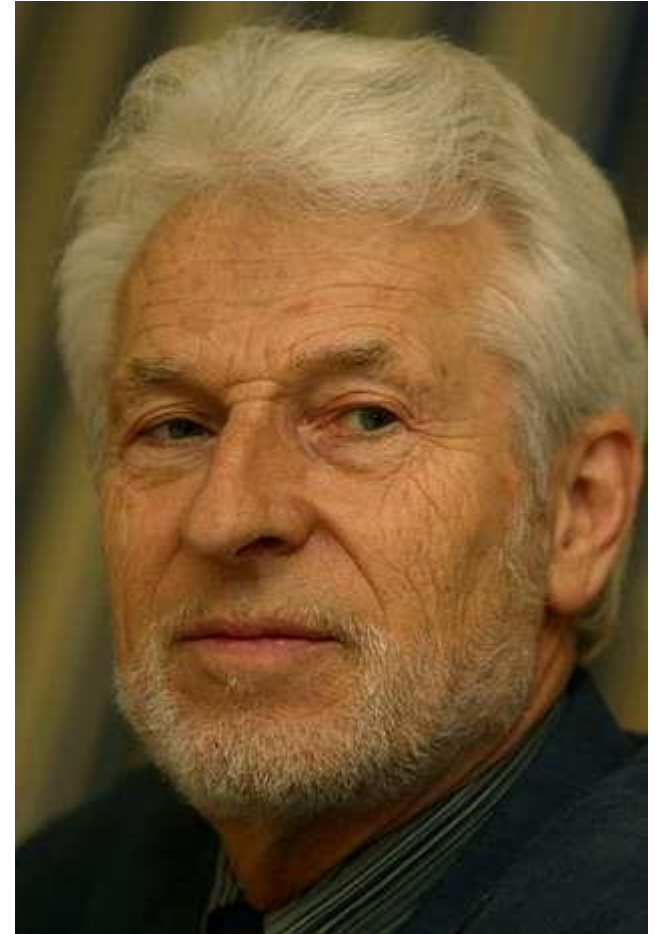


Roche and Sober concede that screening-off isn't an appropriate test for purely logical facts, like entailment relationships.

But they insist that *explanation is more than a purely logical relationship*.

Recall Van Fraassen's argument that a confirmational explanatoriness bonus renders one vulnerable to a Dutch book.

The Roche and Sober argument is supposed to show that such a bonus is impossible, without appealing to a Dutch book argument.



What if explanatoriness plays a role in the priors?

- Today's priors are yesterday's posteriors
- First priors are assigned on the basis of no observation

So much the worse for Bayesianism?

If defenders of IBE want explanatoriness to play a role in confirmation,
they need to formulate a non-Bayesian theory of confirmation.

Gems



You know what they're going to do just by reading the title



Short and sweet



Many potential objections considered

Questions and Critique

- Is proposition E the sort of proposition that can participate in a probabilistic analysis?
- If explanatoriness is more than a logical relationship between H and O —say, a relationship rooted in material facts—then won't "observing" E involve observing new facts that will influence the posterior of H ?
- Recall Lipton's thesis that explanatory loveliness is a *guide* to probabilistic likeliness. Does the Roche/Sober argument contend with this idea?
- IBE is used to *contrast different hypotheses*: more explanatory hypotheses are supposed to be better (confirmed) than less explanatory ones. It seems extremely odd to contrast a hypothesis with *itself* in conjunction with E .