ECO 2795 Notes on reliability It is often claimed that microgrids can provide a more reliable power spily than the good. To study whether or not this statement is true we reld to inderstand some basic concepts of relizability theory let's consider first that we are studying a particular device or component of a system Reliability is the probability that an item will operate without failure for a stated period of the under specified conditions Since reliability is a probability it can only take values between 0 and 1 We identify the reliabity of on item with R The complement of the reliability is the unreliability F. F=1-R Unrelidoility It is the possesself that a coporthype fails to work continuously over a stated time The use of the words "without failure" in the definition of peliation lity or the term "continuously" in the definition of

unreliability is not arbitrary. They imply that the concept of reliability can only be applied directly to Systems or repairable items.

The terms that consider a system's or a repairable item's

Scheviour in normal operation and after a failure are availability

and un availability" and un evailability" The term "ovailability" can be used in different senses defending on The type of system or item 1) Kvailzbil; ty(A) is the probability that a system literal works on demand > Definition appropriate for 2) Dvailzbility (AH) is the probability that a cystemlike is working at a specific time to Definition appropriate for continuous by operating systems 3) Dvailzbility (A) is the expected portion of the time that a system or item performs its required conchon Definition appropriate for repairable
systems On avaliability - It is the probability that a system or ita A=1-Va

Simple model for system behavior State = State - Cailed

Process

Process · Reliability calculation: Fl+1= P(z given item fails in [0, t)) (1) Continuous operation is implicit VIII is a probability distribution with random The probability dansity function is C(t)-dF(t) CHIdt = P[z given item fails in (t, t+dt)) then PUI dt = F(t+dt)- F(x) or FUL (6/16)d6 A hazard function helt) is created to draractorite the transition to the failed state hit is the expected rate

Siven that" 4 CHIdt - P(En iten fails betweent mot tidt / it has not pailed until t) Since P(A/B)= P(A/B)
Plb) But any item that cails between t and t +dt has not failed before so P(ANB) = PLA). Hence, held the B" httldt=P(component fails between t and ttdt)
P(no failure in (o, t)) And, from (1) and (2) h l+1 d+ - Cl+1 dt - h l+1= f(+)
1-F(+)
1-F(+) State of the state

Typical Bin for hitt. no in electronic sombonent Components E LIFE EXPECTANCY Useful life period life zr out period

constant typical failure causes:

failure rate()

typical failures: random

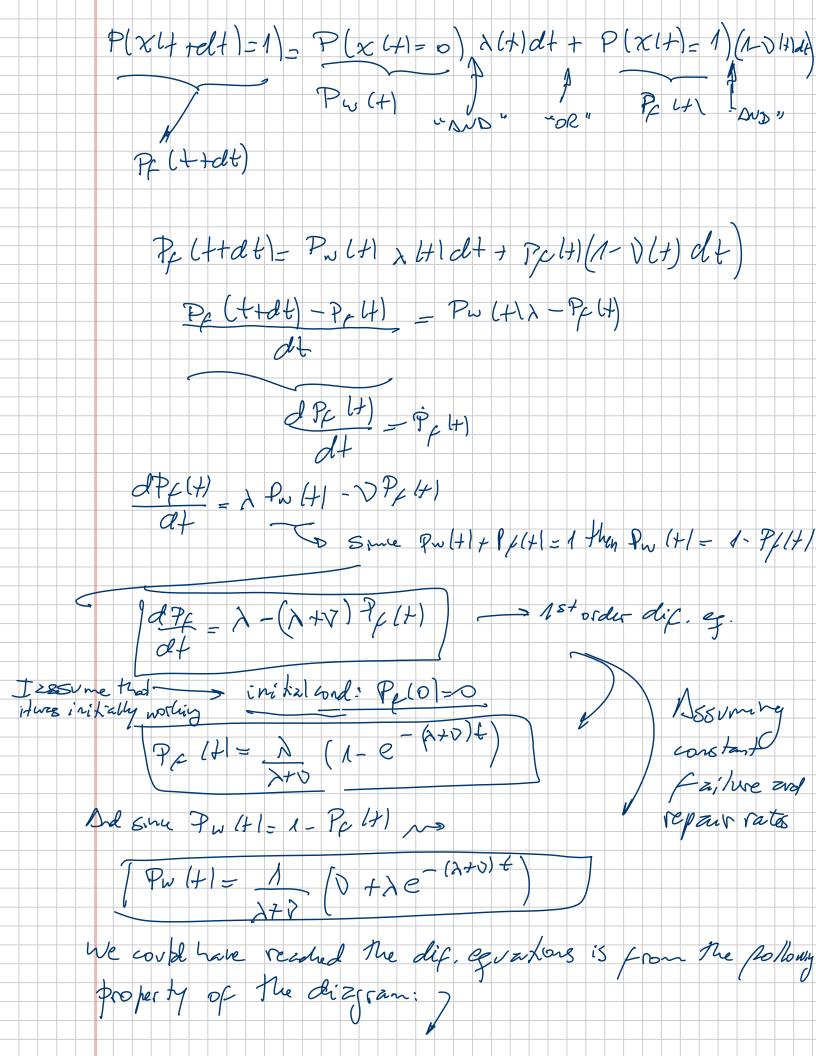
corrosion

chress related oxidation Burn-in period typical failure causes: - poor welding - loose connections With U(t) = \(\tau = \tau \) constant - units: 1 or 1 or 1 year. $F(t) = 1 - e^{-\lambda t} \qquad \Rightarrow c(t) = \lambda e^{-\lambda t}$ $R(t) = e^{-\lambda t}$ The mean is $niff = lis = \int f(t)dt = 1$ Man the to failure Now consider that an item or system can be regarred after it failed and be brought back into service

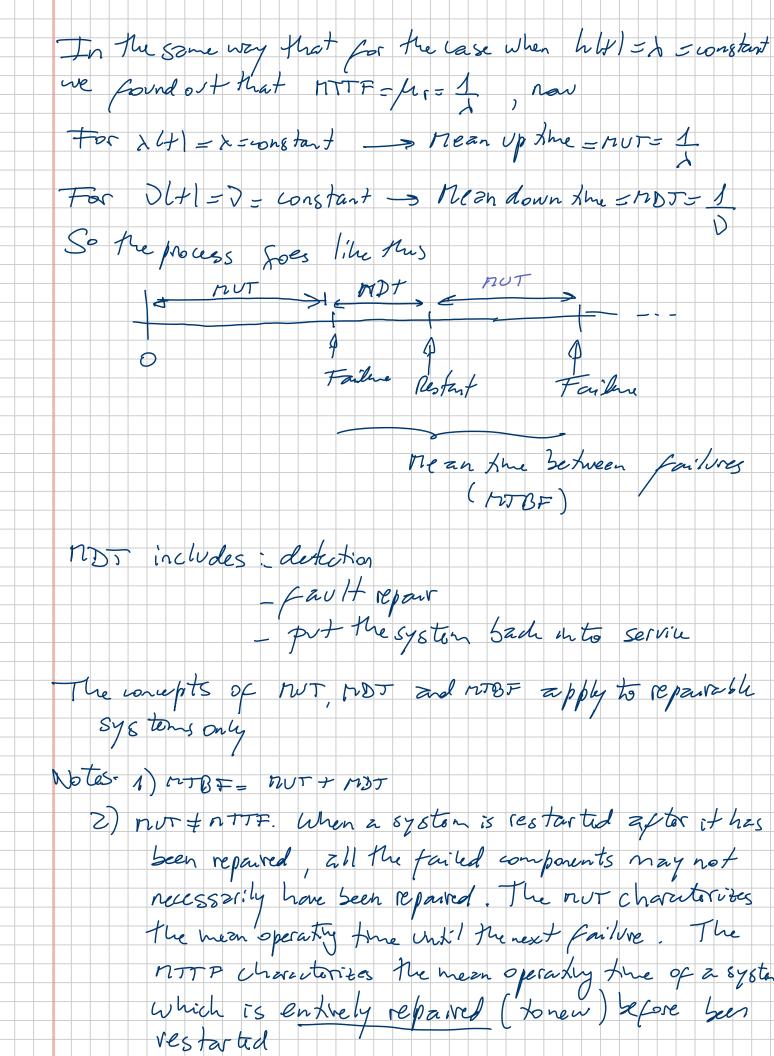
There are several ways to study the reliability behavor of a system or repairable item. A good one is by using Marhor analysis Secure it pravides a graphical deportion of The process and a flexible way of addressing lifterent 5 Nations, The equivalent of the hozzard rate in repairable processes is the pailure rate 2(+) Althor: PC component fails in (t, t+dt))
PC component was working at 6=t) Too the repair process, the equivalence to 2 1/11s the repair rate VII). A simple Marlov's representation of a single repairable component process is: Adt F Adt Adt Adt Working State

Working State

L X 41-1 (3 x 4) =0 XIII _ s State. The probability that the zbreiten is in the failed Stale Consvailzs: lity) after dt is given by: P(x(t+d+)=1) = P(cten was worky at t= E pro unlegoes failure during alt of the component
was failed at to t and it wasn't
repaired during at



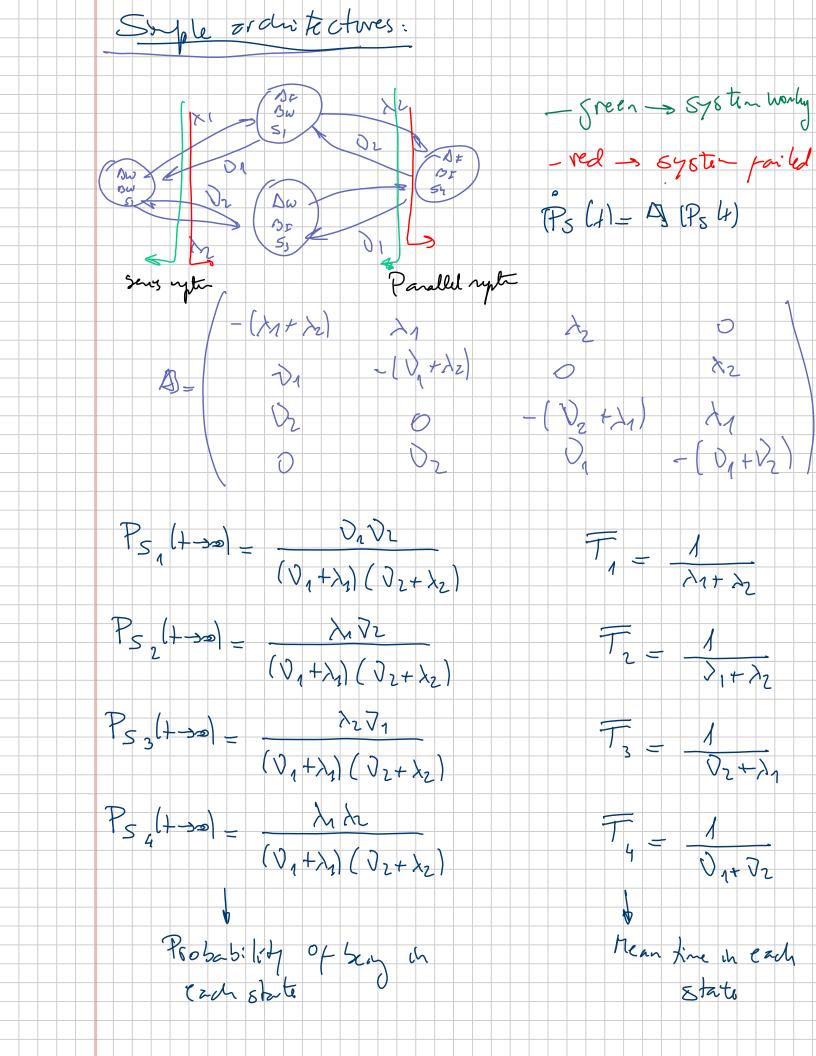
dPstate - (Rate of entering the state) - (Rzto of leaving the state) Interns of Rates, Marhov's diagram becomes: Pw= DP=(+) - X Pw (+) If we plot Pflt ad Pult) we obtain: Steady state probabilities of sen failed or working. I.e. how likely it is that after having seen there" for a long three the it has it working or not. This fits The definitions of Evailability and Unavailability. Here,

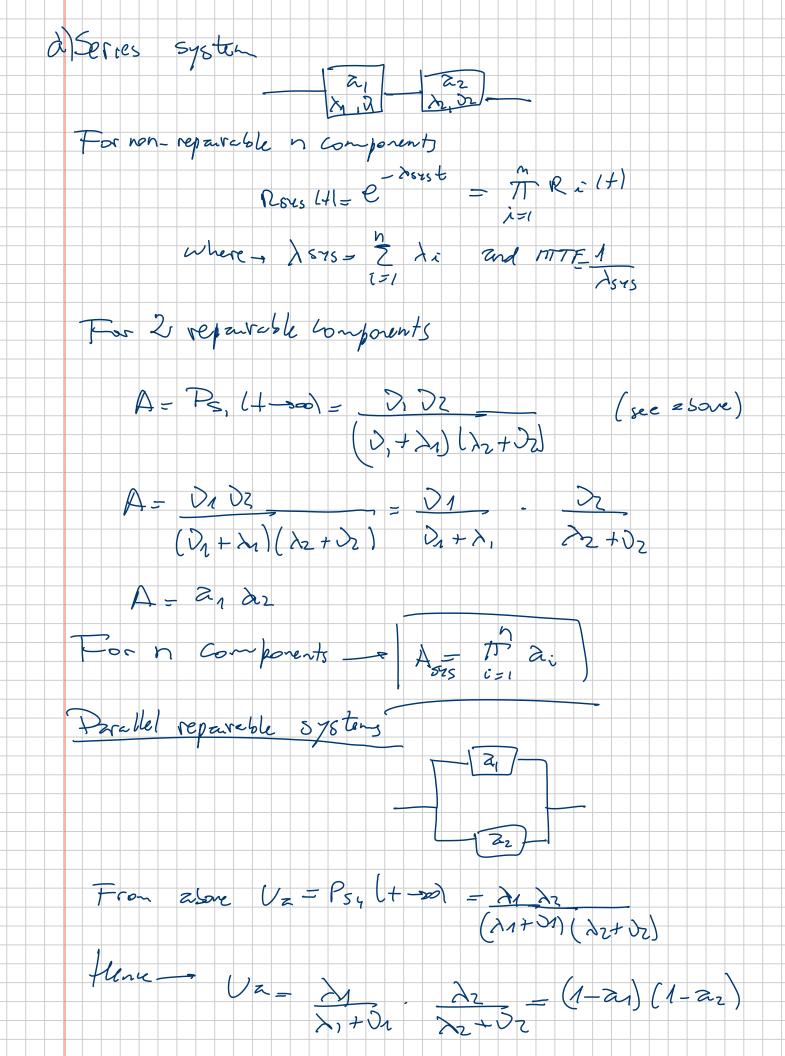


A = 7 - 1 - 1 - 1 - 1 NUT MIBF UP2 WAI Vz - MDF Reliability networks is another technique to calculate ovarilatily of Dystens with multiple components. A reliability hetwork is a representation of the reliability dependencies between components of a system The network has always the following lestires: b) On Ending mode c) A set of rodes d) A sot of edges

e) Do incidence concitor that associates each

esse with an ordered pair of nodes The edges represent the components The nodes represent system architecture
The expected operating andition of the system is represented
by paths though the network. Node to the Endry noch Then The System is working If not the system has pailed

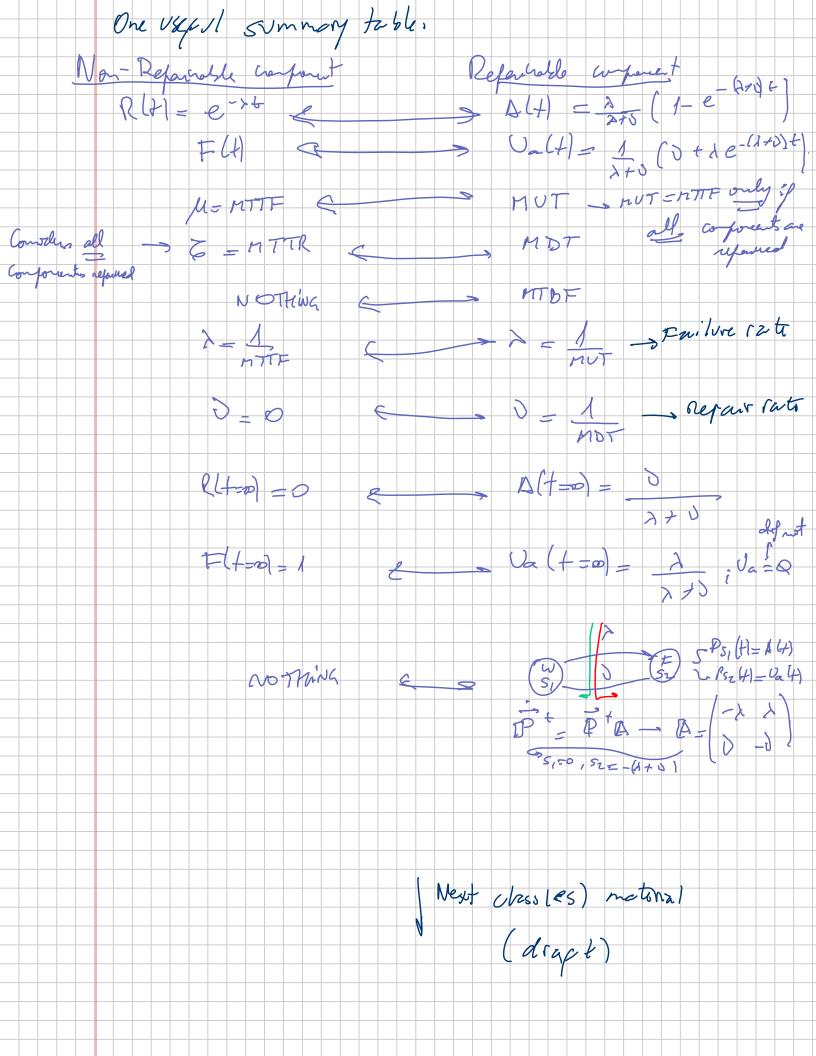




For	n comparents in //
ntl re	dundany
Supp.	se now that we have a modular system with t power to and each module has are rated
Pm.	Then without redundancy we need
	$n = \frac{1}{2} \frac{P_0}{P_m}$
	& The upper integes value of Bo
	e. S. Po = 7 lew / n 54 Pm = 2 lew / n 54
The pr	oblem with 12d of redundary is that if one
power	oblem with 12th of redundary is that if one fails then there is not enough capacity the load.
	e reeded. Then
7405	
	the not a column languist is secured that a column to
modu	ith not I redundany it is required that n of the not les work for full system operation
Then,	

Asis = PC Systen working)= -P (n modules worky) + P (n+1 modules workny) _ nt Cn a Ma + Cn+1 a n+1 All possible Estangement Of At1 elements taken in Svaps of n where the order Binoni al doesn't nather to distryvish among zongements distributed a > zvailability of each module Ma -> Un zvanilability of each module > I can think of the process 25 hours on trials and reguling h or more successes for the 878 ten to work Recall that $2+1 \le (n+1)! = (n+1)! = (n+1)! = n+1$ So Asys = (n+1) Mz + a) 2 = (n+1) (1-a) + a) 2 h Is (n+1) redundancy always better than other options? Consider a fuel cell with a = 0,97 and variable number

of modules: -0.99 0.985 0.98 0.975 0.97 0.9650.96 0.955 L So as the number of modules increase the 578 ton 2 varibbig deligases. so the letta redundant sest reliability capacity represented by option is 1+1" The +1" is less this extra capacity has it cost (\$/hwmodule) perallel. > But modules are larger and the cetra equality is very large (CEVa/s the hoad) One option to improve economics is to se the extra coparity to power something else other than the load. For exemple the love power Can be injected back into the groot and a this way expromes are improved.



Based on these techniques we can calculate a microsside availability. For example, let's consider the y For example, Collowing " Returbine The availetifity can be calculated with the let vrbine aut 20 ting Asys = 2 mg aut 2 c What if we have a more complicated structures we can use Marlion analysis or we am ise the corrept of pallis in = relicitify network: a) Path set: A list of edges such that if they all work, then the system is also in the working state, i.e., any path between the start node and the end node. b) Minimal path set: A path set such that if any one item is removed, the system will no longer work, i.e., any given path between the start node and the end node assuming that all other paths are interrupted due to at least one failed component. c) Cut set: A list of components such that if all fail then the system is also in the failed state. d) Minimal cut set (K): A cut set such that if any one item is removed from the list, the system will no longer fail. The probability that a minimal cut set will occur is given by

$$P(K) = \prod_{i=1}^{N_k} u_i$$

where u_i is the unavailability of the *i*-th edge of the N_k components in the minimal cut set K.

For a system with repairable components, the unavailability can be calculated from [277]

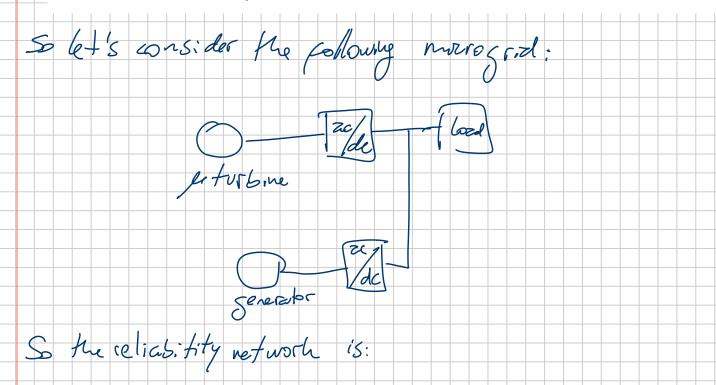
$$U = \mathbf{P}\left(\bigcup_{j=1}^{M_c} K_j\right)$$

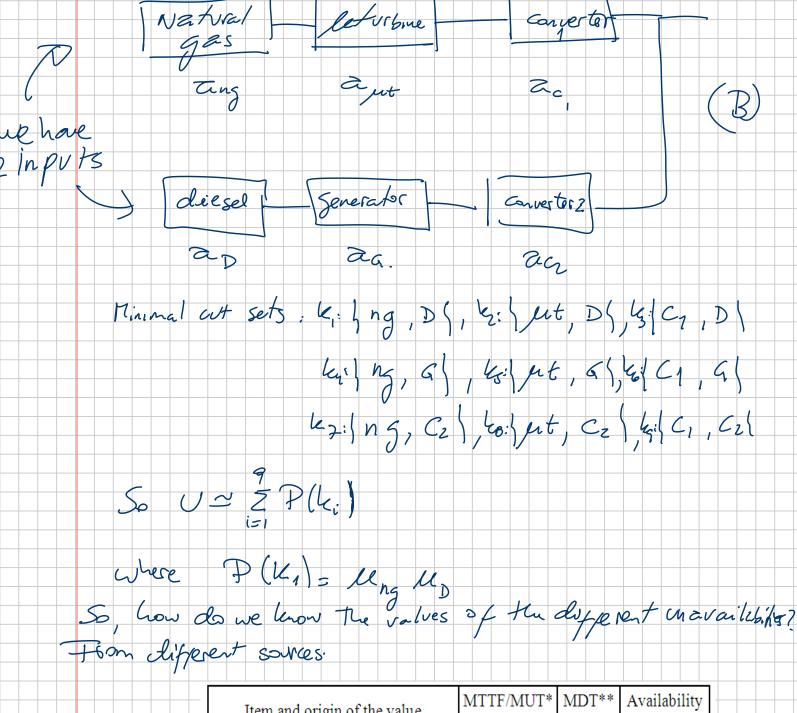
where Mc is the number of minimal cut sets in the system. Calculation of (B.6) is usually extremely tedious. However, the calculation can be simplified by recognizing that U is bounded by

$$\sum_{i=1}^{M_{\varepsilon}} P(K_i) - \sum_{i=2}^{M_{\varepsilon}} \sum_{j=1}^{i-1} P(K_i \bigcup K_j) \le U \le 1 - \prod_{i=1}^{M_{\varepsilon}} [1 - P(K_i)] \le \sum_{i=1}^{M_{\varepsilon}} P(K_i)$$

Thus, if the components are highly available, i.e., $q_i \ll 1$, then U can be approximated to

$$U \cong \sum_{i=1}^{M_c} \mathrm{P}(K_j)$$





Item and origin of the value	MTTF/MUT* (Hours)	MDT** (hours)	Availability <i>a</i>
Reciprocating Engine	823	5	0.9939
PV arrays ****	3636	14	0.996
Fuel Cell (performance degradation)	5000	166.6	0.967742
Microturbine	8000	50	0.993789
Wind turbine ****	1900	80	0.9595
ac mains	2440	2.08	0.999150
Diesel / Gas	2 M	50	0.999975

*MUT: Mean up-time (used for repairable system components)

^{**}MDT: Mean down-time (only applicable to repairable components)

^{***}NR: Not repairable

^{****}Operational MUT and MDT depend on the actual energy availability

For the convertors we can calculate the Evanbability
by estmating the MDT and by calculating the MUTI-MITE FION PATTE - 1 where I can can be calculated by considering that
from a reliability perspective all components are in series. Here The values of λ : can be obtained from the normhal Part Description -> From reliability Resistor Information from: Capacitor Ceramic prediction hand body Capacitor Tantalum Diode such as klosdia J. Kippen. "Evaluating the Transistor Reliability of DC/DC 19.0 SR-237 =d Converters." Sept. 2003, 20.0 [Unfort notely no longer zvailable in Internet) MOSFET MIL-4004=217 IC (20 Transistors) 19.0 Expected by temperative and electrical stress (e.g. white (Krels) Somp / To The Production quality to Usually=1 nominal valve 11 - semperative factor TTE - electrical stress

- Derhenius rate model TT -> Temperature lactor Tr Ts stress

Tr = C)

Reference temporature (le _ Boltzman constant 8.167.15 ev/4 Ea - failure activation energy - depends on Cailure mechanic Calculation of ME: Stress Level Part Description 25% 70% 80% Capacitor Ceramic Capacitor Tantalum 0.48 2.01 2.85 1.00 1.00 1.00 MOSFET IC (25 Transistors) 1.00 1.00 1.00 1.00 1.00 1.00 IC (70 Transistors) IC (150 Transistors) 1.00 1.00 1.00 1.00 1.00 1.00 Final note: Fault tolerant strategies (to avoid Single point of failines): Redundancy: Henry more of the minimum number
of the same system components Diversity: Havy multiple paths Distributed systems: Spread & critical junction