

**This model was developed in the following paper.**

Kurapati, N.; Pathirathna, P.; Chen, R.; Amemiya, S. "Voltammetric measurement of adsorption isotherm for ferrocene derivatives on highly oriented pyrolytic graphite." *Anal. Chem.* **2018**, *90*, 13632.

**This model is also applicable to the system discussed in the following paper.**

Chen, R.; Najarian, A. M.; Kurapati, N.; Balla, R. J.; Oleinick, A.; Svir, I.; Amatore, C.; McCreery, R. L.; Amemiya, S. "Self-inhibitory electron transfer of the Co(III)/Co(II)-complex redox couple at pristine carbon electrode." *Anal. Chem.* **2018**, *90*, 11115.

**CV Model.** A model for CV is based on the adsorption of a ferrocene derivative, FcXY, on HOPG, which proceeds its oxidation to Fc<sup>+</sup>XY as given by



Diffusion equations for FcXY and Fc<sup>+</sup>XY are given by

$$\frac{\partial c_i}{\partial t} = D \left( \frac{\partial^2 c_i}{\partial x^2} \right) \quad (3)$$

where the diffusion coefficient of FcXY,  $D$ , is equivalent to that of Fc<sup>+</sup>XY,  $D_{\text{Fc}^+\text{XY}}$ . The rate of heterogeneous electron transfer,  $v_{\text{et}}$ , is given by the Butler-Volmer model as

$$v_{\text{et}} = k_{\text{red}} c_{\text{Fc}^+\text{XY}} - k_{\text{ox}} c_{\text{FcXY}} \quad (4)$$

with

$$k_{\text{red}} = k_0 \exp \left[ -\alpha_{\text{ET}} F (E - E^{0'}) / RT \right] \quad (5)$$

$$k_{\text{ox}} = k_0 \exp \left[ (1 - \alpha_{\text{ET}}) F (E - E^{0'}) / RT \right] \quad (6)$$

where  $k_{\text{red}}$  and  $k_{\text{ox}}$  are oxidation and reduction rate constants,  $k_0$  is the heterogeneous standard electron-transfer rate constant,  $\alpha_{\text{ET}}$  is transfer coefficient,  $E$  is the HOPG potential, and  $E^{0'}$  is the formal potential

of the redox couple. The substrate potential is cycled between  $E_{\text{initial}}$  and  $E_{\lambda}$  as the switching potential.

The adsorption rate of FcXY,  $v_{\text{ads}}$ , is given phenomenologically by

$$v_{\text{ads}} = k_{\text{ads}} c_{\text{FcXY}} (\Gamma_s - \Gamma_{\text{FcXY}}) - k_{\text{des}} \Gamma_{\text{FcXY}} \quad (7)$$

with

$$k_{\text{ads}} = k_{\text{ads}}^0 \exp(2\alpha_{\text{ads}} g \Gamma_{\text{FcXY}} / RT) \quad (8)$$

$$k_{\text{des}} = k_{\text{des}}^0 \exp[-2(1 - \alpha_{\text{ads}}) g \Gamma_{\text{FcXY}} / RT] \quad (9)$$

$$g = g' RT / 2\Gamma_s \quad (10)$$

where  $k_{\text{ads}}^0$  and  $k_{\text{des}}^0$  are standard adsorption and desorption rate constant,  $\Gamma_{\text{FcXY}}$  is the surface concentration of FcXY,  $g$  is the energy of interaction between adsorbed molecules, and  $\alpha_{\text{ads}}$  is a symmetry coefficient ( $0 < \alpha_{\text{ads}} < 1$ ) regulating the effect of  $g$  on the adsorption activation barrier. Adsorption equilibrium is achieved at  $t = 0$  to yield the Frumkin isotherm based on the Bragg–Williams approximation as given by

$$c_{\text{FcXY}} = \frac{\Gamma_{\text{FcXY}} / \Gamma_s}{\beta(1 - \Gamma_{\text{FcXY}} / \Gamma_s)} \exp(-g' \Gamma_{\text{FcXY}} / \Gamma_s) \quad (11)$$

where  $c_{\text{FcXY}}$  is the concentration of ferrocene derivatives near the HOPG surface,  $\Gamma_s$  is the saturated surface concentration of FcXY, and  $\beta(= k_{\text{ads}}^0 / k_{\text{des}}^0)$  and  $g'$  are parameters characterizing the magnitude of ferrocene–HOPG and ferrocene–ferrocene interactions, respectively. Accordingly, boundary conditions at the substrate surface are given by

$$D \left[ \frac{\partial c_{\text{FcXY}}}{\partial x} \right]_{x=0} = v_{\text{et}} - v_{\text{ads}} \quad (12)$$

$$D \left[ \frac{\partial c_{\text{Fc}^+\text{XY}}}{\partial x} \right]_{x=0} = -v_{\text{et}} \quad (13)$$

$$\left[ \frac{\partial \Gamma_{\text{FcXY}}}{\partial t} \right] = v_{\text{ads}} \quad (14)$$

Finally, a current response for CV,  $i$ , is given by

$$i = FS_{\text{el}} v_{\text{et}} \quad (15)$$

**Dimensionless CV Model.** The aforementioned diffusion problem was redefined by using dimensionless parameters and solved by using a commercial finite element simulation package, COMSOL Multiphysics 5.4 (COMSOL, Burlington, MA). Specifically, eq 3 yielded

$$\frac{\partial C_i}{\partial \tau} = \left[ \frac{\partial^2 C_i}{\partial X^2} \right] \quad (16)$$

where

$$C_i = c_i / c_0 \quad (17)$$

$$\tau = Fvt / RT \quad (18)$$

$$X = x \sqrt{\frac{Fv}{RTD}} \quad (19)$$

Dimensionless parameters were also introduced for boundary conditions (eqs S-8–S-10) to obtain

$$\left[ \frac{\partial C_{\text{FcXY}}}{\partial X} \right]_{X=0} = V_{\text{et}} - V_{\text{ads}} \quad (12)$$

$$\left[ \frac{\partial C_{\text{Fc}^+\text{XY}}}{\partial Z} \right]_{X=0} = -V_{\text{et}} \quad (13)$$

$$\left[ \frac{\partial \theta_{\text{FeXY}}}{\partial \tau} \right] = \frac{V_{\text{ads}}}{K} \quad (14)$$

where

$$K = \frac{\Gamma_s}{c_0} \sqrt{\frac{Fv}{DRT}} \quad (15)$$

In these boundary conditions, the electron-transfer rate was normalized to yield

$$V_{\text{et}} = \Lambda_{\text{het}} \left[ (\theta_{\text{ET}})^{-\alpha_{\text{ET}}} C_{\text{Fe}^+\text{XY}} - (\theta_{\text{ET}})^{1-\alpha_{\text{ET}}} C_{\text{FeXY}} \right] \quad (16)$$

with

$$\Lambda_{\text{het}} = k_0 \sqrt{\frac{RT}{DFv}} \quad (17)$$

The adsorption rate was given in the dimensionless form as

$$V_{\text{ads}} = \Lambda_{\text{ads}} (\theta_{\text{ads}})^{\alpha_{\text{ads}}} C_{\text{FeXY}} (1 - \theta_{\text{FeXY}}) - \Lambda_{\text{dse}} (\theta_{\text{ads}})^{\alpha_{\text{ads}}-1} \theta_{\text{FeXY}} \quad (18)$$

with

$$\Lambda_{\text{ads}} = k_{\text{ads}}^0 \Gamma_s \sqrt{\frac{RT}{DFv}} \quad (19)$$

$$\Lambda_{\text{des}} = k_{\text{des}}^0 \frac{\Gamma_s}{c_0} \sqrt{\frac{RT}{DFv}} \quad (20)$$

Adsorption equilibrium was achieved at  $t = 0$  to yield

$$\frac{\Lambda_{\text{ads}}}{\Lambda_{\text{des}}} = \frac{\theta_{\text{FeXY}}}{1 - \theta_{\text{FeXY}}} \exp(-g' \theta_{\text{FeXY}}) \quad (21)$$

Overall,  $V_{\text{et}}$  is equivalent to a normalized current response,  $I$ , to yield

$$I = V_{\text{et}} = \frac{i}{FS_{\text{el}}c_0} \sqrt{\frac{RT}{DFv}} \quad (22)$$

where  $FS_{\text{el}}c_0\sqrt{DFv/RT}$  is a scaling factor and  $V_{\text{et}} = 0.4463$  for a reversible CV without adsorption.

**Table 1. Parameters Used in COMSOL and Dimensionless Models.**

Parameters		Equation
COMSOL	Dimensionless Model	
Esw	$E_{\lambda} - E^0$	
Erangle	$E_{\lambda} - E_{\text{initial}}$	
k0	$\Lambda_{\text{het}} = k_0 \sqrt{\frac{RT}{DFv}}$	17
theta0	$K = \frac{\Gamma_s}{c_0} \sqrt{\frac{Fv}{DRT}}$	15
Lamda	$\frac{\Lambda_{\text{ads}}}{\Lambda_{\text{des}}}$	19 and 20
g	$g' = 2g\Gamma_s / RT$	10
kappa	$\Lambda_{\text{ads}} = k_{\text{ads}}^0 \Gamma_s \sqrt{\frac{RT}{DFv}}$	19
alpha	$\alpha_{\text{ET}}$	5 and 6
beta	$\alpha_{\text{ads}}$	8 and 9
gamma	$D_{\text{Fc}^+\text{XY}} / D$	