Fast Total Ordering for Modern Data Centers

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Abstract—The performance profile of local area networks has changed over the last decade, but many practical group communication and ordered messaging tools rely on core ideas invented over a decade ago. We present the Accelerated Ring protocol, a novel ordering protocol that improves on the performance of standard token-based protocols by allowing processes to pass the token before they have finished multicasting. This performance improvement is obtained while maintaining the correctness and other beneficial properties of token-based protocols.

On 1-gigabit networks, a single-threaded daemon-based implementation of the protocol reaches network saturation, and can reduce latency by 45% compared to a standard token-based protocol while simultaneously increasing throughput by 30%. On 10-gigabit networks, the implementation reaches throughputs of 6 Gbps, and can reduce latency by 30-35% while simultaneously increasing throughput by 25-40%. A production implementation of the Accelerated Ring protocol has been adopted as the default ordering protocol for data center environments in Spread, a widely-used open-source group communication system.

I. INTRODUCTION

Data center applications rely on messaging services that guarantee reliable, ordered message delivery for a wide range of distributed coordination tasks. Totally ordered multicast, which (informally) guarantees that all processes receive messages in exactly the same order, is particularly useful for maintaining consistent distributed state in systems as diverse as financial systems, distributed storage systems, cloud management, and big data analytics platforms.

Many ordering protocols have been developed to build such messaging services. Défago et al. survey these total ordering protocols and classify them based on their ordering mechanisms [1]. A particularly successful type of ordering protocol is the class of *token-based* protocols.¹ Token-based protocols typically arrange the processes participating in the protocol in a logical ring and order messages using a special control message (called the token) that carries the information needed to order new messages and is passed around the ring. A participant may send messages when it receives the token and is able to assign sequence numbers to its messages before sending them (using the information carried by the token), so messages are ordered at the time they are sent.

Token-based protocols are attractive because of their simplicity; a single mechanism, the token, provides ordering, stability notification, flow control, and fast failure detection. Moreover, these protocols naturally support flexible semantics and continuous operation with well-defined guarantees during network partitions. Token-based protocols also achieved high network utilization at the time they were introduced; for example, the Totem Ring protocol [2] achieved about 75% network utilization on 10-megabit Ethernet using processors standard for 1995. The simplicity, flexibility, and high performance of token-based protocols led to their use in practical messaging services, including the Spread toolkit [3], the Corosync cluster engine [4], and the Appia communication framework [5], [6].

Non-token-based ordering protocols (e.g. Paxos- or sequencer-based) are widely used in practical services, but these approaches often offer subtly different semantics, so the protocols are not entirely interchangeable. We discuss successful systems based on a variety of ordering mechanisms in Section V, commenting on their semantics and performance.

Modern data center environments present different networking and processing trade-offs than in the past, creating performance challenges for protocols relying on core ideas invented over a decade ago. When Fast Ethernet replaced 10megabit Ethernet, network speed increased by a factor of ten, and network span shrank by the same factor (from 2000 to 200 meters). This kept basic network characteristics essentially the same, allowing the same protocols to continue to utilize the network well. However, on networks common in today's data centers, these protocols do not reach the same network utilization as in the past while maintaining reasonable latency.

We were exposed to this problem through our experience with applications using Spread, a widely-used, publicly available group communication toolkit that provides flexible semantics for message delivery and ordering, using a variant of the Totem Ring protocol. Spread reached about 80% network utilization on 100-megabit Fast Ethernet, using processors common for 2004 [7]. However, out-of-the-box, we measured the latest Spread release prior to our work as reaching 50% network utilization on a 1-gigabit network. Careful tuning of the flow control parameters allows Spread to reach 800 Mbps in throughput, but the cost in latency is very high.

One reason that protocols originally designed for 10megabit Ethernet maintained their high network utilization with low latency on 100-megabit Fast Ethernet but not on 1-gigabit, 10-gigabit, and faster networks, is that these faster networks could not use the same techniques as Fast Ethernet to scale throughput (this would have required a 1-gigabit network span to be limited to 20 meters). Moving to these faster networks required changing the network architecture and adding buffering to switches. This changed networking trade-offs. While throughput increased by a factor of 10, 100, or more and latency was substantially reduced, the decrease in latency was significantly lower than the corresponding improvement in throughput.

¹Défago et al. split token-based protocols into *moving sequencer* and *privilege-based* protocols. We use the term *token-based* to refer primarily to privilege-based protocols.

This change in the trade-off between a network's throughput and its latency alters the performance profile of token-based protocols, as these protocols are particularly sensitive to latency. The ability to multicast new messages rotates with the token, so no new messages can be sent from the time that one participant finishes multicasting to the time that the next participant receives the token, processes it, and begins sending new messages. Note that we are concerned with latency intrinsic to the network, not with latency due to particular machines running slowly. In production deployments, we can ensure that the ordering middleware has the resources it needs (e.g. with real-time priorities in Linux).

For processors common today, 10-gigabit and faster networks change trade-offs further by making networking considerably faster relative to single-threaded processing. Unlike in the past, this trade-off is not likely to change soon, as the processing speed of a single core is no longer increasing at a rate comparable to the rate of improvement in network throughput, with Moore's law reaching its limit.

The gap between the performance of existing protocols and the performance that is possible in modern environments led us to design the Accelerated Ring protocol. The Accelerated Ring protocol compensates for, and even benefits from, the switch buffering that limits the network utilization of other tokenbased protocols. Using a simple idea, the Accelerated Ring protocol is able to improve both throughput and latency compared to existing token-based protocols without significantly increasing the complexity or processing cost of the protocol. The Accelerated Ring protocol is still able to take advantage of the token mechanism for ordering, stability notification, flow control, and fast failure detection.

Single-threaded implementations of the protocol are able to saturate 1-gigabit networks and considerably improve performance on 10-gigabit networks without consuming the CPU of more than a single core. Limiting CPU consumption to one core is important for this type of ordering service, as it is intended to serve applications that may be CPU intensive; a service that consumes most of the processing power of the machine is likely to be limiting in many practical deployments.

Like other (privilege-based) token-based protocols, the Accelerated Ring protocol passes a token around a logical ring, and a participant is able to begin multicasting upon receiving the token. The key innovation is that, unlike in other protocols, a participant may release the token before it finishes multicasting. Each participant updates the token to reflect all the messages it will multicast during the current rotation of the token around the ring before beginning to multicast. It can then pass the token to the next participant in the ring at any point during the time it is multicasting. Since the token includes all the necessary information, the next participant can begin multicasting as soon as it receives the token, even if its predecessor on the ring has not yet finished multicasting.

However, the fact that the token can reflect messages that have not yet been sent requires careful handling of other aspects of the protocol. For example, messages cannot be requested for retransmission as soon as the token indicates that their sequence numbers have been assigned, since this may result in many unnecessary retransmissions: a participant may not have received all the messages reflected in the token, not because they were lost, but because they were not yet sent.

Sending the token before all multicasts are completed allows the token to circulate the ring faster, reduces or eliminates periods in which no participant is sending, and allows for controlled parallelism in sending. As a result, the Accelerated Ring protocol can simultaneously provide higher throughput and lower latency than a standard token-based protocol.

We evaluate the Accelerated Ring protocol in a librarybased prototype, a daemon-based prototype, and a production implementation in Spread. Spread has existed for many years, serving production systems since 1998. Examples of current use in 2016 include cloud management, distributed storage products, networking hardware, and financial trading systems. The demands of real applications introduced features that incur significant costs, such as large group names, support for hundreds of clients per daemon, and multi-group multicast (the ability to send a message to all members of multiple distinct groups, with ordering guarantees across groups). Therefore, we also evaluate the protocol in a simple, library-based prototype to quantify the benefit of the protocol outside of a complex system, with no overhead for client communication.

However, part of Spread's success is due to its clientdaemon architecture. This architecture provides a clean separation between the middleware and the application, allows a single set of daemons in a data center setup to support several different applications, and allows open group semantics (a process does not need to be a member of a group to send to that group). Because of this, we additionally evaluate the protocol in a daemon-based prototype that does not incur the cost of all Spread's complexity but provides a realistic solution, including client communication, for a single group.

We compare each implementation of the Accelerated Ring protocol to a corresponding implementation of the original Totem Ring protocol. Sending messages with 1350-byte payloads, on 1-gigabit networks, the Spread implementation of the Accelerated Ring protocol reaches network saturation (over 920 Mbps measuring only payload), and can reduce latency by 45% compared to the original protocol, while simultaneously increasing throughput by 45-60%. On 10-gigabit networks, Spread reaches 2.3 Gbps, and can improve both throughput and latency by 10-20%. The daemon- and library-based prototypes reach 3.3 Gbps and 4.6 Gbps, respectively, and can simultaneously improve latency by 20-35% and throughput by 25-50%. With 8850-byte payloads, throughput reaches 5.2 Gbps for Spread, 6 Gbps for the daemon-based prototype, and 7.3 Gbps for the library-based prototype.

The contributions of this work are:

- 1) The invention of the Accelerated Ring protocol, a new ordering protocol that takes advantage of the trade-offs in modern data center environments.
- A thorough evaluation of the protocol in a library-based prototype, a daemon-based prototype, and Spread on 1gigabit and 10-gigabit networks.



(b) Accelerated Ring Protocol

Fig. 1. Executions of the original Ring protocol and the Accelerated Ring protocol. White boxes are data messages; black boxes are token messages. Numbers represent the sequence number on data messages and the sequence field on the token.

3) The release of the Accelerated Ring protocol as part of Spread's open-source code, and the adoption of this protocol as Spread's standard ordering protocol for local area networks and data center environments.

An extended abstract about this work appeared in [8], and additional experimental results can be found in [9].

II. SYSTEM AND SERVICE MODEL

The Accelerated Ring protocol provides reliable, totally ordered multicast and tolerates message loss (including token loss), process crashes and recoveries, and network partitions and merges. We assume that Byzantine faults do not occur and messages are not corrupted.

The Accelerated Ring protocol provides Extended Virtual Synchrony (EVS) semantics [10]. EVS extends the Virtual Synchrony (VS) model [11] to partitionable environments. EVS, like VS, provides well-defined guarantees on message delivery and ordering with respect to a series of configurations. A configuration consists of a set of connected participants that can communicate among themselves but not with participants outside that set, and a unique identifier for the configuration.

The Accelerated Ring protocol provides *Agreed* and *Safe* delivery services. These services are completely and formally specified in [10], but the most relevant properties are:

- Agreed delivery guarantees that messages delivered within a particular configuration are delivered in the same total order by all members of that configuration. The total order respects causality.
- Safe delivery guarantees that if a participant delivers a message in some configuration, each member of the configuration has received that message and will deliver it, unless it crashes. This property is often called *stability*.

The protocol can also provide FIFO and Causal delivery services, but their latency is similar to that of Agreed delivery. Therefore, they are not discussed here.

III. ACCELERATED RING PROTOCOL

The complete Accelerated Ring protocol consists of an ordering protocol and a membership algorithm. Since the

Accelerated Ring protocol directly uses the membership algorithm of Spread, which is based on the Totem membership algorithm [2], we focus on the ordering protocol, which is novel, in this paper. However, both components are necessary to support the above system model and service semantics.

The following description specifies the normal-case operation of the Accelerated Ring protocol with a static set of participants. We assume that the membership of the ring has been established, and the first regular token has been sent. Crashes, network partitions, and token losses are not discussed here, as they are handled by the unmodified membership algorithm; the Accelerated Ring protocol does not introduce any new failure modes relative to the original Ring protocol.

A. Overview

Figure 1 shows an example execution with three participants sending a total of twenty messages in the original Totem Ring protocol and the Accelerated Ring protocol.

In the original protocol (Figure 1a), each participant sends five messages when it receives the token and then passes the token to the next participant. The token carries the sequence number of the last message that was sent, so the next participant knows exactly which sequence numbers it can assign to its messages. For example, when Participant B receives the token with sequence number 5 from Participant A, it can send message 6, since it knows that no sequence number higher than 5 has been assigned to a message.

In the accelerated protocol (Figure 1b), each participant similarly sends five data messages upon receiving the token, but it sends some of those messages *after* passing the token to the next participant. In this example, each participant sends its first two data messages, then sends the token, and then sends its last three data messages. Note, however, that the token carries exactly the same sequence numbers as in the original protocol. Even though Participant A does not send messages 3, 4, and 5 until after it has passed the token to Participant B, it has already decided exactly which messages it will send. Therefore, the token that Participant B receives still carries the sequence number 5, reflecting all the messages that Participant A will send during the current rotation of the token around the ring (also called a *token round*). Just as in the original protocol, Participant B learns that no sequence number higher than 5 has been assigned to a message and can send messages with sequence numbers starting at 6. Unlike protocols that improve performance by providing a speculative result before reaching a full agreement on ordering like Zyzzyva [12] or ToTo [13], the Accelerated Ring protocol marks each message with its final sequence number at the time it is sent. A participant will not deliver message 6 until it receives all messages 1-5 and can deliver it in the correct order.

To see how the Accelerated Ring protocol simultaneously improves throughput and latency, notice that the accelerated protocol takes less time to complete a token round than the original protocol. Figure 1 clearly shows that the first 15 messages are sent and the token is returned to Participant A earlier in the accelerated protocol than in the original protocol. The Accelerated Ring protocol improves throughput by sending the same 15 messages in less time and improves latency by getting the token back to Participant A faster, so it waits less time to send message 16. The parallelism that gives us this performance improvement is enabled by the buffering of modern switches discussed in Section I.

To gain an intuition for the correctness of the accelerated protocol, notice that if Participant B receives messages 1 and 2 but not messages 3-5 before receiving the token in the execution of the Accelerated Ring protocol in Figure 1b, then from Participant B's point of view, that execution is exactly like the execution of the original Ring protocol in the case that messages 3-5 are lost, and the original Ring protocol copes with message loss. However, in the original protocol, Participant B would then immediately request messages 3-5 for retransmission. In the accelerated protocol, these messages are most likely in transit, rather than lost, so requesting them would lead to unnecessary retransmissions and reduce performance. Therefore, in the Accelerated Ring protocol, we request missing messages one round after noticing them, guaranteeing that they have already been sent and should have arrived. Thus, the improved throughput and latency of the Accelerated Ring protocol comes at the cost of requiring an extra round to recover lost messages (but each round is faster).

The number of messages a participant can send when it receives the token depends on the *Personal_window* parameter: the maximum number of new data messages a participant can send in one token round. The *Accelerated_window* specifies the maximum number of these messages that can be sent *after* passing the token. In Figure 1b, the *Personal_window* is five and the *Accelerated_window* is three. If a participant has fewer than *Personal_window* messages to send, it still sends as many as possible after the token. If a participant in Figure 1b only had two messages to send, it would send both after the token.

Below we describe the Accelerated Ring protocol in detail. During normal operation, participants take actions in response to receiving token messages and data messages. We describe how these messages are handled in Sections III-B and III-C.

B. Token Handling

Token messages carry control information that is used to establish a correct total order and provide flow control. Token messages contain the following fields:

- 1) *seq*: Last sequence number assigned to a message. When a participant receives a token, it can multicast new messages with sequence numbers starting at seq + 1.
- 2) aru (all-received-up-to): Field used to determine the highest sequence number such that each participant has received every message with a sequence number less than or equal to that sequence number. Messages all participants have received can be delivered with Safe delivery semantics and/or garbage-collected.
- 3) fcc (flow control count): Total number of multicast messages sent during the last token round (including retransmissions). Participants use this field when determining the maximum number of messages they may send in the current round.
- 4) *rtr* (retransmission requests): List of sequence numbers corresponding to messages that must be retransmitted (because they were lost by some participant).

The steps a participant executes upon receiving a token are:

- Pre-token multicasting: calculating the total number of messages to send and multicasting messages, including all retransmissions and potentially some new messages (Section III-B1)
- 2) Updating and sending the token (Section III-B2)
- 3) Post-token multicasting: multicasting new messages that the participant decided on but did not multicast during pre-token multicasting (Section III-B3)
- 4) Delivering and discarding messages (Section III-B4)

1) Pre-token Multicasting: The participant first retransmits any messages it has that are requested in the *rtr* field of the token. All retransmissions must be sent during the pre-token phase; otherwise, they may be unnecessarily requested again.

The participant then calculates *Num_to_send*, the total number of new messages it will multicast in the current round. *Num_to_send* is the minimum of the number of data messages the participant currently has to send and the number of messages it is allowed to send while respecting the flow control parameters: the *Personal_window* specifies the maximum number of new data messages a single participant can send in one token round, while the *Global_window* specifies the maximum total number of data messages that can be sent in a single token round by all participants combined.

Finally, the participant may multicast some of its new messages. Each new message is stamped with its sequence number (assigned consecutively, starting at *seq* + 1) before it is sent. The number of new messages sent in the pre-token phase depends on the *Accelerated_window*, which specifies the maximum number of messages a participant can send *after* passing the token. The number of new messages a participant sends in the pre-token phase is *Num_to_send* – *Accelerated_window*. If *Num_to_send* is less than or equal to the *Accelerated_window*, the participant sends no new messages in the pre-token phase.

2) Updating and Sending the Token: Before passing the token to the next participant in the ring, the current token holder updates each of the token fields.

The *seq* field is updated by adding *Num_to_send* to the value of the *seq* field on the received token. This sets the *seq* field to the highest sequence number that has been assigned to a message.

The *aru* field is updated according to the rules in [2]. Each participant tracks its local *aru*, which is the highest sequence number such that the participant has received all messages with sequence numbers less than or equal to that sequence number. If the participant's local *aru* is less than the *aru* on the token it receives, it lowers the token *aru* to its local *aru*. If the participant lowered the token *aru* in a previous round, and the received token's *aru* has not changed since the participant lowered it, it sets the token *aru* equal to its local *aru*. If the received token's *aru* and *seq* fields are equal, and the participant does not need to lower the token's *aru*, it adds *Num_to_send* to the *aru* on the token it received.

The *fcc* field is also updated as in [2]. The total number of retransmissions and new messages the participant sent in the previous round are subtracted from the received token's *fcc* value, and the total number of retransmissions and new messages the participant is sending in the current round are added to the received token's *fcc* value.

The *rtr* field is updated to remove retransmission requests that the participant answered in this round and add requests for any messages that this participant has missed. The fact that participants can pass the token before completing their multicasts for the round complicates retransmission requests, since the *seq* field of the token may include messages that have not actually been sent yet. In order to avoid unnecessarily retransmitting messages, the participant only requests retransmissions for missing messages up through the value of the *seq* field on the token it received in the *previous* round, rather than the token it just received.

The updated token is then sent to the next participant.

3) Post-token Multicasting: During this phase, the participant completes its sending for the current round. If Num_to_send is less than the Accelerated_window, it sent no new messages during the pre-token phase and sends all of these messages (if any) during the post-token phase. Otherwise, it sends Accelerated_window data messages during this phase.

4) Delivering and Discarding: As the final step of token handling, the participant uses the procedure in [2] to deliver and discard messages. A participant can deliver a Safe message once it has received and delivered all messages with lower sequence numbers and knows that all other participants have received and will deliver the message (unless they crash). Therefore, the participant delivers all messages with sequence numbers less than or equal to the minimum of the *aru* on the token it sent this round and the *aru* on the token it sent last round. Since every participant had the opportunity to lower the *aru* during the round, every participant must have a local *aru* of at least the minimum of these two values. Since every

participant has these messages, they will never be requested for retransmission again and can also be discarded.

C. Data Handling

Data messages carry application data to be multicast, as well as meta-data used for ordering messages. Each data message contains the following fields:

- 1) *seq*: Sequence number of this message. This specifies the message's position in the total order.
- 2) pid: ID of the participant that initiated this message.
- *round*: Token round in which the message was initiated.
 payload: Application data. This is not inspected or used by the protocol.

When a participant receives a data message, it inserts it into its buffer of messages, ordered by sequence number. If the message allows the participant to advance its local *aru* (i.e. the sequence number of the message equals its local *aru* + 1), it delivers its undelivered messages in the order of their sequence numbers until it reaches a sequence number higher than the local *aru* (i.e. a message it has not received) or a message requiring Safe delivery. Messages requiring Safe delivery cannot be delivered until the token *aru* indicates that they have been received by all participants.

D. Selecting a Message to Handle

In general, token and data messages are handled as they arrive. However, when messages arrive nearly simultaneously, both token and data messages can be available for processing at the same time. The protocol decides which to handle first by assigning logical priorities to message types. When a message type has *high priority*, no messages of the other type will be processed as long as some message of that type is available.

The key issue is that a participant should not process a token until it has processed all the data messages reflected in the last token it processed (or as many as it will receive, if there is loss). If these messages have not yet been processed, but were not lost, they will be unnecessarily requested. However, in order to maximize performance, the token should be processed as soon as possible. Note that decisions about when to process messages of different types can impact performance but do not affect the correctness of the protocol.

A participant always gives data messages high priority after processing a token. However, two different methods may be used to decide when to raise the token's priority again after processing the token for a given round. In the first method, a participant gives the token high priority as soon as it processes any data message its immediate predecessor in the ring sent in the next token round (indicated by the *round* field of the data message). In the second method, a participant waits to give the token high priority until it processes a data message that its immediate predecessor sent in the next round *after* having sent the token for that round. The first method maximizes the speed of token rotation. The second slows the token slightly to reduce the number of unprocessed data messages that can build up but maintains the acceleration of the token by raising its priority as soon as it is known to have been sent.



Fig. 2. Agreed delivery latency vs throughput, 1 Gb network

E. Implementation Considerations

Our implementations of the Accelerated Ring protocol use IP-multicast to transmit data messages and UDP unicast to pass the token. We use IP-multicast since it is generally available in the local area networks and data center environments for which the protocol is designed, especially when building infrastructure (in contrast to applications hosted on the cloud). However, if IP-multicast is not available, unicast can be used to construct logical multicast at the cost of reduced performance; this capability is available as an option in Spread.

In the prototypes, we use the first, more aggressive method for giving the token high priority, since this gives the best performance with properly tuned flow-control parameters. However, for Spread we chose the second, less aggressive method, because this method is less sensitive to misconfiguration, which is important for open-source systems used in a wide variety of production environments. When the *Accelerated_window* is zero, the second method behaves like the original Ring protocol, while the first method may still accelerate the token by processing it as early as possible.

IV. EVALUATION

We evaluate the performance profile of the Accelerated Ring protocol experimentally and compare it to the performance of the original Totem Ring protocol [2]. We evaluate both protocols in library-based and daemon-based prototypes as well as in complete production implementations in Spread. The performance of non-token-based ordering approaches is discussed in Section V.

A. Benchmarks

All benchmarks use 8 Dell PowerEdge R210 II servers, with Intel Xeon E3-1270v2 3.50 GHz processors, 16 GB of memory, and 1-gigabit and 10-gigabit Ethernet connections. The servers were connected using a 1-gigabit Catalyst 2960 Cisco switch and a 10-gigabit 7100T Arista switch.

To evaluate each protocol, we ran the system at varying throughput levels (measured in clean application data only), ranging from 100 Mbps up to the maximum throughput of the system. At each throughput level, we measured the average latency to deliver a message for both Agreed and Safe delivery.



Fig. 3. Safe delivery latency vs throughput, 1 Gb network

For Spread and the daemon-based prototype, each of the 8 participating servers ran one daemon, one sending client that injected messages at a fixed rate, and one receiving client. Each sending client sent the same number of messages, and each receiving client received all the messages sent by all sending clients. For the library-based prototype, each server ran one process that injected and received messages.

A broad range of parameter settings provide good performance. *Personal_windows* of a few tens (e.g. 20-40) of messages with *Accelerated_windows* of half to all of the *Personal_window* yield good results in all environments we tested. We report results with the smallest *Personal_window* and corresponding *Accelerated_window* that let the system reach its maximum throughput.

1) 1-gigabit Experiments: For these experiments, all data messages contained a 1350-byte payload. This size allows the entire message to fit in a single IP packet with a standard 1500-byte MTU, while allowing sufficient space for protocol headers. Spread requires large headers to support features needed by users, such as descriptive group and sender names.

Figures 2 and 3 show the relationship between throughput and latency for Agreed and Safe delivery, respectively. These figures show a clear difference between the profiles of the original Ring protocol and the Accelerated Ring protocol, across all implementations. When Spread uses the original protocol, its latency for Agreed delivery is at least 400 μ s, even for the lowest throughput level tested (100 Mbps). In contrast, with the accelerated protocol, Spread is able to reach 400 Mbps throughput with latency below 400 μ s. At 900 Mbps, Spread's latency is under 1.2 ms using the accelerated protocol, which is about the same as the latency for the original protocol at 400 Mbps. With the original protocol, Spread supports up to 500 Mbps, with latency around 1.3 ms, before latency begins to climb rapidly. The accelerated protocol supports 800 Mbps with latency around 720 μ s, simultaneously improving throughput by 60% and latency by over 45%.

The accelerated protocol also improves maximum throughput compared to the original protocol. Using the accelerated protocol, Spread reaches over 920 Mbps. Since we measure only clean application data, and Spread adds substantial headers, this is practically saturating the 1-gigabit network.

Safe delivery shows a similar pattern. For all implementa-





Fig. 5. Agreed delivery latency vs throughput for 1350 byte messages and 8850 byte messages, 10 Gb network

tions, the original protocol supports up to 600 Mbps before latency begins to rise sharply, and latency is 3.7 - 4.7 ms at this point. The accelerated protocol supports 800 Mbps with latency around 2 ms, improving throughput by over 30% and latency by over 45% at the same time. The accelerated protocol achieves throughput over 900 Mbps with latency comparable to that of the original protocol at 600 Mbps.

2) 10-gigabit Experiments: Figures 4 and 6 show performance profiles from the same experiments as in Figures 2 and 3, but on a 10-gigabit network. For Agreed delivery, using the original protocol, Spread can provide throughput up to about 1 Gbps before the protocol reaches its limits and latency climbs. Its average latency at this throughput is 385 μ s. Using the accelerated protocol, Spread can provide 1.2 Gbps throughput with an average latency of about 310 μ s, for a simultaneous improvement of 20% in both throughput and latency. The maximum throughput Spread reaches with latency under 1 ms using the original protocol is 1.6 Gbps, but using the accelerated protocol, Spread is able to reach 2 Gbps with similar latency, for a 25% improvement in throughput.

Unlike on 1-gigabit networks, on 10-gigabit networks, processing is slow relative to the network. Therefore, the differing overheads of the different implementations significantly affect performance. While Spread can support 1.2 Gbps throughput with latency around 310 μ s using the accelerated protocol, the daemon-based and library-based prototypes support up to 2.9 Gbps and 3.5 Gbps, respectively, at the same latency.

Because processing is a bottleneck for Spread on 10gigabit networks, the prototype implementations better show



Fig. 6. Safe delivery latency vs throughput, 10 Gb network



Fig. 7. Safe delivery latency vs throughput for 1350 byte messages and 8850 byte messages, 10 Gb network

the power of the protocol. For the daemon-based prototype, the original protocol supports 2 Gbps with latency around 390 μ s. The accelerated protocol supports 2.8 Gbps throughput with latency around 265 μ s, for a simultaneous improvement of 40% in throughput and over 30% in latency.

The performance profile for Safe delivery is similar but with higher overall latencies for the stronger service. Using the original protocol, Spread supports 1.1 Gbps throughput with an average latency of 930 μ s; using the accelerated protocol, Spread can support the same throughput with 25% lower latency (about 700 μ s), achieve 20% higher throughput with the same latency (about 1.35 Gbps), or improve both throughput and latency by about 10% each (with latency of about 810 μ s for 1.2 Gbps throughput).

As for Agreed delivery, the difference between the protocols is even clearer for the prototype implementations. For the daemon-based prototype, the original protocol supports 2.5 Gbps throughput with 1.5 ms latency, while the accelerated protocol supports 3.1 Gbps with 980 μ s latency, improving throughput by 25% and latency by 35% at the same time.

Using the accelerated protocol, Spread achieves a maximum throughput of 2.3 Gbps (a 35% improvement over the original protocol's maximum of 1.7 Gbps), the daemon-based proto-type reaches 3.3 Gbps, and the library-based prototype reaches 4.6 Gbps.

The accelerated protocol always provides lower latency than the original protocol for the same throughput in 1-gigabit experiments or for Agreed delivery. However, Figure 8 shows that for Safe delivery on 10-gigabit networks the original protocol can provide better latency than the accelerated protocol at very low aggregate throughputs. This is because raising the token *aru* can cost up to an extra round in the accelerated protocol (because the *aru* typically cannot be raised in step with the token's *seq* value). At low throughputs on 10-gigabit networks, token rounds are already very fast, so the accelerated protocol cannot speed up each round as much, and the extra round becomes significant. At 100 Mbps, Spread's average latency is 620 μ s with the accelerated protocol, which is nearly 20% higher than the original protocol's 520 μ s. However, once throughput reaches 4-5% of the network's capacity (400-500 Mbps), the accelerated protocol consistently provides lower latency.



Fig. 8. Safe delivery latency for low throughputs, 10 Gb network

3) 10-gigabit Experiments with Larger UDP Datagrams: On 10-gigabit networks, processing power becomes the limiting factor, preventing both the original Ring protocol and the Accelerated Ring protocol from fully utilizing the network. If higher throughput is needed, one approach is to amortize processing costs over larger message payloads. Spread includes a built-in ability to pack small messages into a single protocol packet, but the size of a protocol packet is limited to fit within a standard 1500-byte MTU; large messages are fragmented into multiple packets. However, we can use UDP datagrams of up to 64 kilobytes, allowing message fragmentation to be done at the kernel level, with the trade-off that losing a single frame causes the whole datagram to be lost.

To evaluate the performance profile of the Accelerated Ring protocol when processing costs are amortized over larger payloads, we ran the same experiments with message payloads of 8850 bytes and UDP datagrams of up to 9000 bytes. This choice is inspired by the 9000-byte jumbo frame size, allowing the same 150 bytes for headers as in the experiments with 1350-byte payloads. We chose not to use jumbo frames at the network level, since they may not be available in all deployments, although they may improve performance further.

Figures 5 and 7 compare the performance profiles of the Accelerated Ring implementations using 1350-byte payloads (as in Figures 4 and 6) to the profiles using 8850-byte payloads. Larger messages allow the protocol to reach considerably higher throughputs. For Agreed delivery, the maximum throughput for Spread improves 150%, from 2.1 Gbps to 5.3 Gbps; for the daemon-based prototype it improves 87%,

from 3.2 Gbps to 6 Gbps; and for the library-based protocol it improves 58%, from 4.6 Gbps to 7.3 Gbps. Because the benefit of larger messages comes from amortizing processing costs, we see the biggest improvements when processing overhead is highest. Figure 7 shows similar improvements for Safe delivery.

4) Experiments Under Loss: To evaluate the protocols under loss, we used the daemon-based prototypes, with each daemon instrumented to randomly drop a certain percentage of the data messages it received. As in the normal-case experiments, we used 8 servers, each running a daemon, a sending client, and a receiving client. Note that because messages are dropped independently at each daemon, the overall rate of retransmissions in the system is much higher than the loss rate at each daemon. In our experiments, the loss rate at each daemon ranged from 0-25%, but the actual rate of retransmissions in the system was typically 5.5 - 6.8 times higher, making this an extremely demanding experiment (the retransmission rate can be greater than 100%, since retransmissions may also be lost). With a loss rate of 25% at each daemon, the probability that a given message does not need to be retransmitted at all is only 13%.

Note that we only consider data-message loss in this evaluation, not token loss. Token loss is handled by the membership algorithm, which is identical for the two protocols. Moreover, token loss is rare, since the token is sent on a different port than data messages and received on a separate socket; since a process only needs to receive one token per round, it should always have sufficient buffer space to receive the token.

Figure 9 shows the effect of loss on latency for both Agreed and Safe delivery. In this experiment, the sending clients sent 1350-byte messages at an aggregate rate of 480 Mbps. This rate is 20% of the throughput the original protocol supports on a 10-gigabit network, which was chosen so that both protocols could support the total throughput of the experiment, even with the retransmissions. The solid lines in the figure show the average latency over all messages, while the dashed lines show the average latency over the worst (i.e. highest latency) 5% of messages from each sender.



Fig. 9. Latency vs loss, 480 Mbps goodput, 10 Gb network

The Figure 9 shows that for both Agreed and Safe delivery, the accelerated protocol has higher average latency than the original protocol once the loss rate reaches 5%. This is expected, since the accelerated protocol waits an extra round to request retransmissions. For Agreed delivery, the accelerated protocol's latency can be up to 47% higher than that of the original protocol. However, for Safe delivery, the difference is only 5-7%. Safe delivery takes longer overall in terms of token rounds, so the fact that the Accelerated Ring protocol reduces the time each token round takes has a larger impact on Safe delivery latency and partially compensates for the extra round needed to request retransmissions.

The highest latency messages include those that need to be retransmitted more than once and those that wait close to a full token round to be sent for the first time (because they arrived from the client at the daemon just after the daemon released the token). As the number of overall rounds increases, the accelerated protocol's advantage of shorter rounds has a greater impact and offsets the additional round needed to request retransmissions. Therefore, for the highest latency messages (dashed lines in Figure 9), the accelerated protocol is slightly more similar to the original protocol in Agreed delivery latency (with up to 26% higher latency) and provides about the same Safe delivery latency as the original protocol.



Fig. 10. Latency vs loss, 1200 Mbps goodput, 10 Gb network

Figure 10 shows the results of the same experiment as Figure 9, but with clients sending at an aggregate rate of 1200 Mbps, representing 50% of the throughput the original protocol supports on a 10-gigabit network. At this throughput level, Safe delivery latency is lower for the accelerated protocol than for the original protocol, while Agreed delivery latency is similar for both under all tested loss rates. At higher throughputs, each token round takes substantially longer in the original protocol, since each daemon has more messages to send in each round and must send them all before releasing the token. Because the accelerated protocol does not force daemons to send all of their messages before releasing the token, increased throughput has less effect on latency.

Figure 11 shows the results of the same experiment but on a 1-gigabit network, with sending clients sending at an aggregate rate of 140 Mbps (20% of the throughput the original protocol supports on a 1-gigabit network). On a 1-gigabit network, the latency improvement from using the accelerated protocol is so great that even with the additional round that the accelerated



Fig. 11. Latency vs loss, 140 Mbps goodput, 1 Gb network

protocol needs to request lost messages, the accelerated protocol provides better latency than the original protocol under all tested loss rates, providing slightly lower latency for Agreed delivery (2-45%) and 22-50% lower latency for Safe delivery, depending on the loss rate.

Focusing on the highest latency messages or sending at higher throughputs shows the same pattern as on 10-gigabit networks – the overall latencies are higher, but the advantage of the accelerated protocol over the original protocol increases. Additional experiments under loss, including higher throughputs on 1-gigabit networks can be found in [9].

B. Discussion

The evaluation clearly shows the benefit of the Accelerated Ring protocol over a standard token-based protocol. Using the accelerated protocol, Spread, with all the overhead of a real system, practically saturates a 1-gigabit network. In fact, it achieves similar or better network utilization than in 2004 on 100-megabit Fast Ethernet [7], with excellent latency.

Using larger UDP datagrams, a library-based prototype is able to achieve about 73% network utilization on a 10gigabit network. This is comparable to the original Totem Ring protocol, which was benchmarked similarly to our librarybased implementation on a 10-megabit network [2]. Thus, a relatively simple but powerful protocol change, plus the use of larger UDP datagrams, allows the same core protocol to scale three orders of magnitude over 20 years.

The current version of Spread uses UDP datagrams that fit in a single frame with a 1500-byte MTU. While we are not considering using jumbo frames in the default configuration, allowing larger UDP datagrams on 10-gigabit networks may be beneficial. A drawback of UDP datagrams that span multiple network frames is that losing a single frame causes the whole datagram to be lost. However, using a protocol with good flow control, like the Accelerated Ring protocol, in a stable local area network, like those in data center environments, we expect loss to be small. Therefore, larger UDP datagrams may be a reasonable trade-off for applications that need both high throughput and all of the features of Spread.

The Accelerated Ring protocol's performance improvement comes at the cost of waiting an extra token round to recover lost messages. While this can make the accelerated protocol's latency higher than that of the original protocol when there is significant loss on the network, the evaluation shows that this effect only appears on 10-gigabit networks at relatively low aggregate throughputs. At higher throughputs or on 1-gigabit networks, the accelerated protocol's latency advantage over the original protocol compensates for the extra round, keeping its overall latency lower than that of the original protocol.

V. RELATED WORK

The Accelerated Ring protocol builds on a large body of work on reliable, totally ordered multicast. Existing protocols vary in the techniques they use to achieve total ordering, as well as the precise semantics they guarantee.

One of the earliest token-based protocols is the protocol of Chang and Maxemchuk [14]. This protocol exemplifies a token-based moving sequencer protocol; the process holding the token assigns a sequence number to each message it receives and sends that sequence number to the other processes. The Pinwheel protocols [15] introduce performance optimizations to the Chang and Maxemchuk protocol.

As previously discussed, the Accelerated Ring protocol is closely related to the Totem Ring protocol [2]. Spread's original protocol is a variant of Totem, and the Accelerated Ring protocol directly uses the variant of the Totem membership algorithm implemented in Spread.

While we chose a token-based approach for its simplicity and flexible semantics, other total ordering mechanisms exist. Défago et al. provide an extensive survey of total ordering algorithms and classify them by their ordering mechanisms [1].

One popular approach to ordering is to use Paxos [16] to order messages by executing a series of consensus instances to assign sequence numbers to messages. This approach has been used to perform replication in many well-known systems, including Boxwood [17], Chubby [18], and Spanner [19].

While Paxos provides total ordering, it does not offer exactly the same semantics as the Accelerated Ring protocol. We designed the Accelerated Ring protocol to maintain the flexible Extended Virtual Synchrony semantics that our experience has shown to be useful in supporting a wide variety of applications. Paxos-like approaches lack this flexibility; they provide a service similar to Safe delivery but cannot provide weaker services for a lower cost, and they require a quorum to make progress. In addition, the total order of Paxos-based approaches does not respect FIFO ordering if a process can submit a new message for ordering before learning that its previous messages were ordered. However, Paxos's semantics are appropriate for many applications, and numerous variants and optimizations have been designed (e.g. [20]–[23]).

Ring Paxos [22] shares our goal of high throughput and uses ring-based communication. It achieves high performance by using efficient communication patterns in which a coordinator multicasts messages to all processes and acknowledgments are forwarded around a logical ring. Multi-Ring Paxos [24] scales throughput by running multiple rings that order messages independently. Processes can deterministically merge messages from multiple rings to obtain a complete total order.

The popular Zookeeper [25] coordination service uses the ZAB [26] protocol for primary-backup replication. ZAB is similar to Paxos but enforces FIFO ordering and provides stronger ordering guarantees across leader failures. Like Paxos, ZAB requires a quorum to make progress.

The ISIS toolkit [27] was one of the first practical group communication systems and was used in air traffic control systems and the New York Stock Exchange, among many other places. ISIS is based on the Virtual Synchrony model and uses vector timestamps to establish causal ordering and a sequencer-based protocol to establish total ordering.

While sequencer-based approaches like the one in ISIS can provide a variety of service levels, their handling of network partitions is typically limited, preventing them from cleanly merging partitioned members. Members that do not belong to a primary component typically need to rejoin as new members. We focus on token-based approaches in part because they can naturally provide rich semantics in a partionable model.

In the Trans protocol [28], used by Transis [29], processes attach positive and negative acknowledgments to messages they multicast. These acknowledgments, along with perprocess sequence numbers, are used to build a directed acyclic graph over the messages, which determines the total order.

These alternative approaches to ordering have also been used to build successful practical messaging systems that achieve good performance on modern networks. JGroups [30] is a popular, highly-configurable messaging toolkit that includes a sequencer-based total ordering protocol, as well as less expensive FIFO ordering. A 2008 evaluation reports that, on a 1-gigabit network, the FIFO protocol achieves 405 Mbps throughput with 1000-byte messages and 693 Mbps with 5000byte messages [31]. Using the setup in Section IV, we measure 650 Mbps throughput for the total ordering protocol on a 1-gigabit network with 1350-byte messages (880 Mbps for FIFO) and 3 Gbps on a 10-gigabit network (4 Gbps for FIFO).

Isis2 [32], [33] is a cloud computing library that includes totally ordered multicast using a sequencer-based protocol, stronger safety guarantees using Paxos, and a weaker, cheaper FIFO multicast. Isis2 allows users to work with replicated distributed objects (automatically maintaining consistent copies).

CORFU [34] is distributed shared log that can provide totally ordered reliable broadcast: each new message is appended to the log, and the order of messages in the log corresponds to the total order. To reduce contention and improve performance, processes reserve a specific log position from a dedicated sequencer before attempting to write to the log. This allows writes to distinct log positions to occur in parallel, which resembles the parallel multicasting enabled by the Accelerated Ring protocol.

U-Ring Paxos [35] adapts Ring Paxos and Multi-Ring Paxos to work without IP-multicast by propagating both acknowledgments and data around the ring. While providing efficient (logical) multicast in the absence of IP-multicast is important for certain environments (e.g. WANs), significant effort has been spent on optimizing IP-multicast and allowing it to support large numbers of groups; our experience has shown that it is reasonable to take advantage of its performance when building infrastructure in data center environments. Using a single ring, U-Ring Paxos is reported to reach over 900 Mbps sending 8000-byte messages on a 1-gigabit network [35], which matches our measurements in the same 8-machine setup described in Section IV. When sending 1350-byte messages (but allowing batching), we measure U-Ring Paxos as reaching over 750 Mbps with a latency profile similar to that of the original Ring protocol for Safe delivery. On a 10-gigabit network, we measure U-Ring Paxos as reaching close to 1.5 Gbps with 1350-byte messages. Higher throughput may be achieved by running multiple rings in parallel, but this requires additional processing resources.

VI. CONCLUSION

We presented the Accelerated Ring protocol, a new protocol for totally-ordered multicast that is designed to take advantage of the trade-offs of 1-gigabit and 10-gigabit networks. The Accelerated Ring protocol significantly improves both throughput and latency compared to standard token-based protocols, while maintaining the correctness and attractive properties of such protocols. The protocol is available as open-source and has been adopted as the default protocol for local area networks and data center environments in the Spread toolkit.

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