Lecture 1

Lecture 1 Inequalities, sets and absolute value

MATH 0200

Dr. Boris Tsvelikhovskiy

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1 Inequalities

2 Sets

3 Intervals



4 Absolute value

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Let a and b be two numbers. We will consider the following relations between them:

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• $a < b, a \le b$ (read 'a is less than b' and 'a is less than or equal to b');

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Properties

• Transitivity: $a \leq b \leq c$ implies $a \leq c$;

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- Transitivity: $a \le b \le c$ implies $a \le c$;
- Multiplication by a constant:
 - if $a \leq b$ and c > 0, then $ac \leq bc$;

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- Addition of inequalities: if $a \leq b$ and $c \leq d$, then $a + c \leq b + d$.

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- Addition of inequalities: if $a \leq b$ and $c \leq d$, then $a + c \leq b + d$.
- If a > b > 0, then $\frac{1}{b} > \frac{1}{a}$.

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Inequalities

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Definition

A set is a collection of objects, satisfying specified properties: $S = \{ \text{objects} \mid \text{properties} \}.$

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Example

• $A = \{\text{animals in Pitt Zoo}\}$

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Example

- $A = \{\text{animals in Pitt Zoo}\}$
- $B = \{$ students at Pitt | student knows sets $\}$

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- $A = \{\text{animals in Pitt Zoo}\}$
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- $C = \{a \in \mathbb{R} \mid a > 2022\}$ is the set of real numbers greater than 2022.

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Inequalities

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Absolute value A very important class of sets is given by intervals. There are three types of intervals.

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(1) Open interval:
$$(a, b) = \{c \mid a < c < b\}.$$

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(1) Open interval:
$$(a, b) = \{c \mid a < c < b\}.$$

(2) Half-open intervals: $[a,b) = \{c \mid a \le c < b\}$ and $(a,b] = \{c \mid a < c \le b\}.$

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- (1) Open interval: $(a, b) = \{c \mid a < c < b\}.$
- (2) Half-open intervals: $[a,b) = \{c \mid a \le c < b\}$ and $(a,b] = \{c \mid a < c \le b\}.$
- (3) Closed interval: $[a, b] = \{c \mid a \le c \le b\}.$

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Here we describe the basic operations on sets. Let A and B be two sets.

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Union: A ∪ B is the set of elements that belong to at least one of the sets A, B.

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Example

Let A = (-1, 4) and B = [-5, 2] be two intervals. Then the union $A \cup B$ is the half-open interval [-5, 4) and the intersection $A \cap B$ is the half-open interval (-1, 2].

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Question

Let $X = \{1, 4, 5, 6, 8, 9, 11\}$ and $Y = \{2, 4, 7, 9\}$ be two sets. What are the union $X \cup Y$ and intersection $X \cap Y$?

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Absolute value

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Interval

Absolute value $|x| = \begin{cases} x, \ x \ge 0\\ -x, x < 0 \end{cases}$

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Example

Find all x satisfying the inequality $|x - 3| \ge 4$.

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Interval

Absolute value The inequality is equivalent to $x - 3 \ge 4$ or $x - 3 \le -4$, which in turn gives the union $x \ge 7 \cup x \le -1$, in the interval notation, $(-\infty, -1] \cup [7, \infty)$.

Example

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Find all x satisfying the inequality $|x - 3| \ge 4$.

The inequality is equivalent to $x - 3 \ge 4$ or $x - 3 \le -4$, which in turn gives the union $x \ge 7 \cup x \le -1$, in the interval notation, $(-\infty, -1] \cup [7, \infty)$.



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