Quiz 4

Your name:

Your TA's name:

- 1. Find the derivatives of the given functions
- (a) [10 points]  $f(x) = 2^{\sin 3x}$

(b) [10 points]  $f(t) = e^{\sec^{-1} t}$ 

| 2. [10 points] A certain radioactive isotope take for 100 grams to decay to 25 grams? | has a half-life | of 5 years. | How many | years will it |
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| 3. [10 points] | Use a linear | approximatic | on (or differe | entials) to est | timate the nu | mber $\sqrt{99.8}$ . |
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Bonus problem for the first midterm [10 points]

Use the Intermediate Value Theorem to show that there is a root of the equation  $\sin x - 1 = -2x$  in the interval  $\left(0, \frac{\pi}{2}\right)$ . Provide all the necessary steps and details.