Spring 2012

Your name:

Math 0220

Your TA's name:

No calculators. Show all your work (no work = no credit). Write neatly.

- 1. (a) [4 points] Determine whether the function $f(x) = \frac{|x|}{\sin x}$ is even, odd or neither.
- (b) [1 point] What is the domain of f(x) inside the interval $[-\pi, \pi]$?

2. [5 points] Evaluate the limit, if it exists. If it does not exist explain why.

$$\lim_{h \to 0^-} \left(\frac{1}{|h|} + \frac{1}{h} \right)$$

In your work mention what Rules, Laws, or Formulas you use.

3. [5 points] Sketch the graph of an example of a function g(x) if it has the domain [-2,6) and satisfies all the given conditions

$$\begin{split} g(-2) &= 1, \quad \lim_{x \to 0^-} g(x) = -2, \quad \lim_{x \to 0^+} g(x) = 2, \quad g(2) \text{ is undefined,} \\ g(3) &= 5, \quad \lim_{x \to 3^-} g(x) = 3, \quad \lim_{x \to 3^+} g(x) = 1, \\ \lim_{x \to 5} g(x) &= -2, \quad g(5) = 2, \quad \lim_{x \to 6^-} g(x) = -1. \end{split}$$

bonus problem [5 points extra] Evaluate the limit, if it exists. If it does not exist explain why.

$$\lim_{\theta \to 0} \frac{\tan(\sin \theta)}{\sin 3\theta}$$