Spring 2012

Your name:

Math~0220

Your TA's name:

No calculators. Show all your work (no work = no credit). Write neatly.

1. [5 points] Evaluate the limit, if it exists. If it does not exist explain why.

$$\lim_{x \to \infty} \cos 2x$$

2. [5 points] Is the function

$$h(x) = \begin{cases} \frac{x^2 - x}{x^2 - 1} & \text{if } x \neq 1\\ 1 & \text{if } x = 1 \end{cases}$$

continuous or discontinuous at a=1? Show why it is continuous (or discontinuous) at this point.

3. [5 points] Using the definition of the derivative find f'(a) if $f(x) = x^2 - 5x$.

bonus problem [5 points extra] Show that any line of nonzero slope that passes through the point (0,1) must intersect the graph of $\sin x$ at least once.