Spring 2012

Your name:

Math 0220

Your TA's name:

No calculators. Show all your work (no work = no credit). Write neatly.

- 1. (a) [3 points] Does the function $f(x) = \frac{x^3 + 64}{x + 4}$ have removable discontinuity at -4. Support your answer.
- (b) [2 points] If the discontinuity is removable, find a function g(x) that agrees with f(x) for $x \neq -4$ and is continuous at -4.

2. [5 points] Evaluate the limit, if it exists. If it does not exist explain why.

$$\lim_{x \to \infty} \left(\sqrt{9x^2 + 2x} - 3x \right)$$

3. [5 points] Sketch the graph of an example of a function g(x) if it satisfies all the given conditions

$$g(0) = 0$$
, $g'(0) = 3$, $g'(1) = 0$, and $g'(2) = -1$

bonus problem [5 points extra] Use the definition of the derivative to compute the derivative of the function g(x) = f(2x) at a number x = a, where f is a differentiable function.