

## Quiz 4

Spring 2012

Math 0280

Your name: \_\_\_\_\_

1. [8 points] The transformation  $T$  stretches a vector by a factor of 2 in the  $x$ -component and by a factor of 3 in the  $y$ -component. Show that the transformation  $T$  from  $\mathbb{R}^2$  to  $\mathbb{R}^2$  is linear by showing that it is a matrix transformation.



2. [7 points] Using the definition of a linear transformation show that

$$T \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} x - y + z \\ 2x + y - 3z \end{bmatrix}$$

is a linear transformation.



bonus problem [5 points extra] Let  $l$  and  $m$  be two lines through the origin and  $F_l$  and  $F_m$  be the corresponding reflections (and linear transformations). Is  $F_l \circ F_m$  also a reflection in a line through the origin. If it is then prove it, if it is not then give a counterexample.

