August 2008, #1: Suppose f is a real-valued continuous, non-constant function on $[a, b]$, $a < b$. Prove that the range of f is a segment [that is, a closed interval $[\alpha, \beta]$ for some $\alpha < \beta \in \mathbb{R}$].