

(9)

Chpt. 3 - Postulates

1. State of QM system completely specified by wavefunction $\Psi(x,t)$

$$P(x_0, t_0) = \Psi(x_0, t_0)^* \Psi(x_0, t_0) dx = |\Psi(x_0, t_0)|^2 dx$$

↑ probability of finding the particle at x_0 at t_0 within dx

$$\int_{-\infty}^{\infty} |\Psi(x,t)|^2 dx = 1 \quad \leftarrow \text{probability of finding the particle somewhere}$$

⇒ Ψ single valued

$\Psi, \frac{d\Psi}{dx}$ continuous

cannot be ∞ over a finite interval

2. Each observable is associated with a QM operator

Position: $\hat{x} = x$

Momentum: $\hat{p}_x = \frac{\hbar}{i} \frac{\partial}{\partial x}$

KE: $\hat{E}_{kin} = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2}$

PE: $\hat{E}_{pot} = V(x)$

total E: $\hat{H} = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} + V(x)$

Ang mom: $\hat{l}_x = \frac{\hbar}{i} \left(y \frac{\partial}{\partial z} - z \frac{\partial}{\partial y} \right)$

...

3. In a single measurement of an observable associated with \hat{A} , only eigenvalues of \hat{A} are measured.

4. Expectation value: $\langle a \rangle = \frac{\int_{-\infty}^{\infty} \Psi^* \hat{A} \Psi dx}{\int_{-\infty}^{\infty} \Psi^* \Psi dx}$

average of the observable a ,
if many measurements are done.

if Ψ is an eigenfunction of \hat{A} , all measurements give the same result.

if Ψ is not an eigenfunction of \hat{A}

$$\Psi = \sum b_n \phi_n(x, t)$$

↑ eigenfunctions of \hat{A}

$$\langle a \rangle = \sum |b_m|^2 a_m, \text{ assuming } \Psi \text{ is normalized}$$

Suppose $\psi(x) = \frac{1}{2} \phi_1(x) + \frac{\sqrt{3}}{2} \phi_2(x)$, ϕ_1, ϕ_2 being eigenfunctions of \hat{A}

$$\hat{A} \phi_1 = a_1 \phi_1, \quad \hat{A} \phi_2 = a_2 \phi_2$$

How frequently do we measure a_1 ? a_2 ?

5. The time evolution of a QM system is given by

$$i\hbar \frac{\partial \Psi(x, t)}{\partial t} = \hat{H} \Psi(x, t)$$

If Ψ is a soln. of the time-independent SE -

$$\Psi = \psi(x) e^{-iE\hbar/\hbar}$$