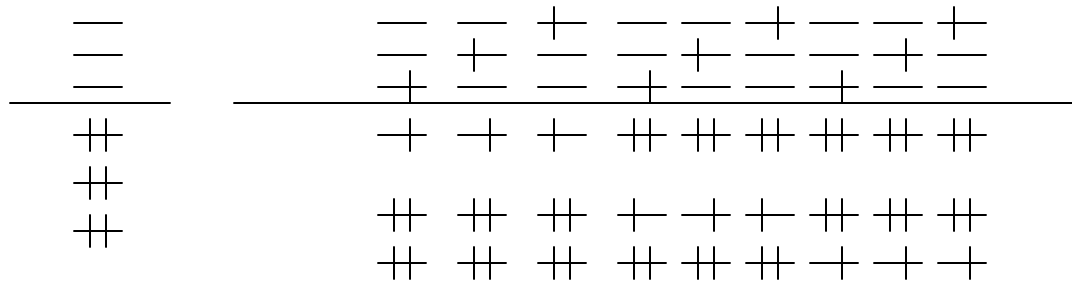


# CIS = “Configuration Interaction Singles”



HF ground state  $\longrightarrow$  use these orbitals to do single excitation CI calculation on excited state

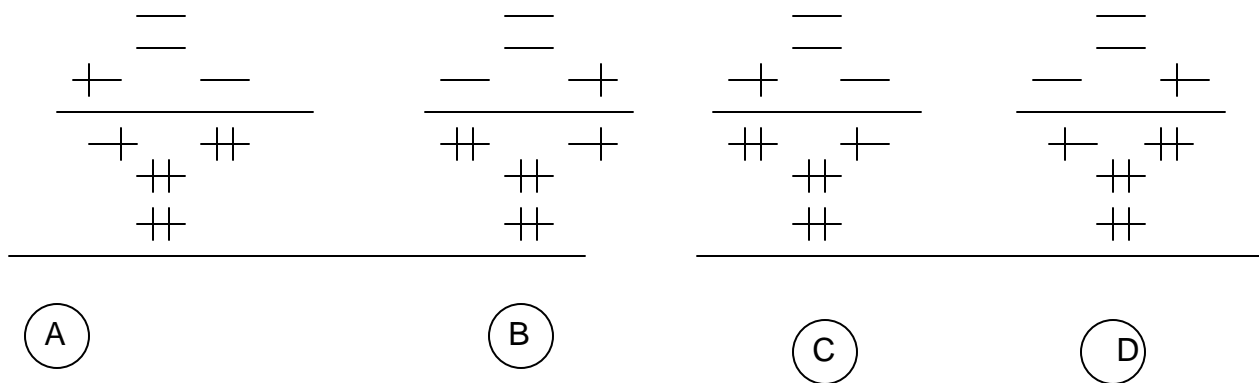
## CIS is not really treating electron correlation

It is essentially an HF calculation on the excited state, allowing for single excitation degeneracies.

It properly handles spin in excited singlet states.

$$A \pm B$$

Now consider benzene



degenerate

degenerate

Proper wavefunctions go like  $A \pm B$  and  $C \pm D$

CIS properly handles this sort of degeneracy

CIS = singlets

triplets

root = N – root for geometry opt.

(default N = 1)

direct (if over 200 basis functions)

Nstates = M (default is 3)

CIS calculations give:

- excited state energies
- excitation energies
- transition moments  $\sim |\langle 0 | \tilde{r} | i \rangle|$
- oscillator strengths  $\sim |\langle 0 | \tilde{r} | i \rangle|^2$
- dipole moments, etc. (using density = current or density = all)

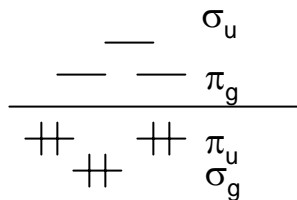
# CASSCF (N, M)

- N = # electrons
- M = # orbitals

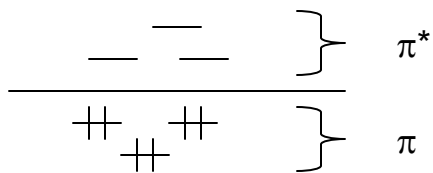
All arrangements  
of N electrons  
in M orbitals

## Examples

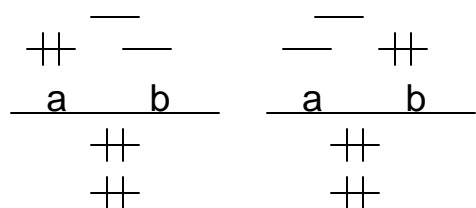
H<sub>2</sub> – CAS (2,2)



N<sub>2</sub> – CAS(6,6)



Benzene – CAS (6,6)



← CAS(2,2) ← especially important for diradicals

$$\begin{aligned}
 \psi &= a^2 - b^2 = (L + R)^2 - (L - R)^2 \\
 &= LF + RL \leftarrow \text{two unpaired electrons} \\
 &\text{singlet diradical.}
 \end{aligned}$$

## Some “tricks” of CASSCF calculations

- Need correct orbitals occupied in initial guess (might need alter)
- #P to get eigenvalues and eigenvectors printed
- NROOT = 1 – optimize the ground state
- CASMP2 – add multireference MP2 correction to CASSCF
- stateguess = k – starting vector for Lanczos method
- Maximum # active orbitals = 12 (fairly expensive)
- Careful – does not use symmetry in setting up the CAS CI matrix

$$\psi = C_1 |1\sigma_g^2| + C_2 |1\sigma_u^2|$$

CASSCF – optimize orbitals + coefficients

lowest possible energy for this type of wavefunction

CI – Fix orbitals, vary coefficients

– Linear variational princ.

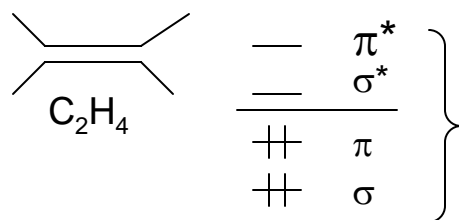
– Matrix eigenvalue problem

Full CI grows factorially

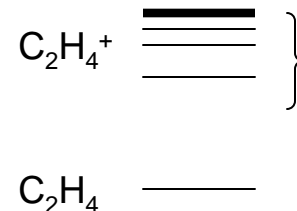
possible for only small systems, e.g., H<sub>2</sub>O

with 3-21G basis set

### Valence vs. Rydberg states



~1/n<sup>2</sup> progression →  
Rydberg series



$\pi \rightarrow \pi^*$ ,  $\sigma \rightarrow \pi^*$ ,  $\pi \rightarrow \sigma^*$   
valence transitions

$\pi \rightarrow 3s$ ,  $\pi \rightarrow 4s$ ,  $\pi \rightarrow 5s$ ,  
 $\pi \rightarrow 3p$ ,  $\pi \rightarrow 4p$ ,  $\pi \rightarrow 3d$

### Observations

- In some cases, lowest valence transitions below lowest Rydberg transitions
- But in some molecules, Rydberg states overlap low-lying valence states
- In fact, molecules such as H<sub>2</sub>O, and CH<sub>4</sub> lack valence excited states.