

Optimizations

Useful to consider Taylor series of PES

$$E(\mathbf{x}) = E(\mathbf{x}_0) + E'(\mathbf{x}_0)(\mathbf{x}-\mathbf{x}_0) + 1/2E''(\mathbf{x}_0)(\mathbf{x}-\mathbf{x}_0)^2$$

Gradient (\mathbf{g})

Hessian (\mathbf{H})

\mathbf{x} , and \mathbf{g} are vectors, \mathbf{H} a matrix

- **Steepest descents** – step downhill in direction given by \mathbf{g}

Very inefficient

- **Newton Raphson** –

$$\Delta\mathbf{x} = -\mathbf{H}^{-1}\mathbf{g}$$

Trouble if there is a zero eigenvalue of \mathbf{H} (need to remove transl. and rot.)

Wrong direction, if neg. eigenvalue

If \mathbf{H} is approximated - quasiNewton

Eigenmode following

- diagonalize H
- $\Delta\mathbf{x} = - \sum F_i \mathbf{V}_i / b_i$
- $\Delta E = - \sum F_i^2 / 2b_i$
 - $b_i =$ eigenvalue
 - $\mathbf{V}_i =$ eigenvector
 - $F_i =$ comp. of g along \mathbf{V}_i
 - Can be used to find TS's!
- $\Delta\mathbf{x} = - \sum F_i \mathbf{V}_i / (b_i - \lambda_i)$ <<shifting>>

The "berny" algorithm in G03 is similar to EF

- Default – simple guess for H
- Updates H as calculation proceeds
- Usually OK for locating minima
- If problems: opt=calcfc, opt=calchfc

Can also partially evaluate numerically

Berny checks # neg. eigenvalues of H

Will stop if incorrect (**can override**)

Convergence

- Max force
- Rms force
- Max. step
- Rms step

To use with z-matrix: opt=z-matrix

```
# hf/3-21G opt=z-matrix test
```

```
Relaxed scan – will do 18 optimizations
```

```
0 1
```

```
O1
```

```
H 1 r1
```

```
C 1 r2 2 a2
```

```
R1 0.9 S 5 0.5
```

```
R2 1.1
```

```
A2 115.4 S 2 1.0
```

Transition states

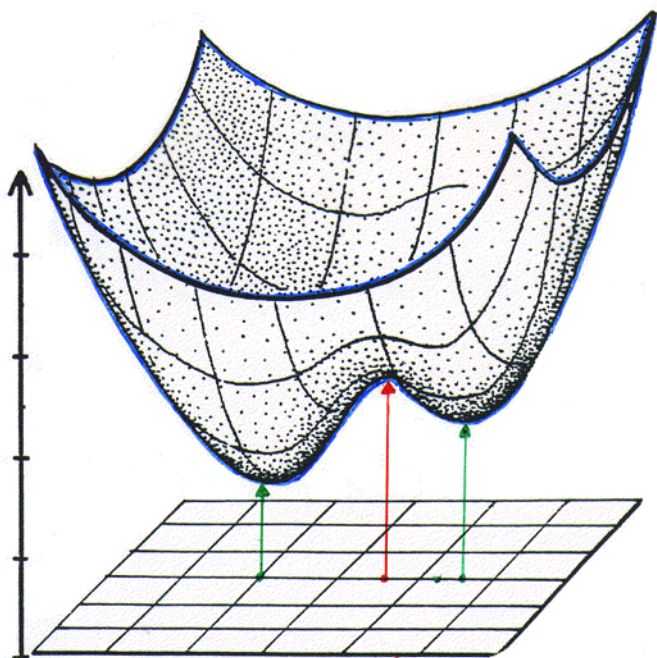
- Easy when determined by symmetry (e.g., OH rotation in phenol)

Can just use constrained minimization

- When not symmetry constrained – tougher than minimization

Need to have a good initial guess structure, and usually curvature info.

- Even when TS is found, non-trivial to find the associated minima



2-dim. PES
with two
minima
and one TS

See: www.tau.ac.il/~becker/course/mini.html

Opt=

- TS (based on berny)

Actually need curvature, e.g., opt=(ts, calcfc)

- (TS,EF)

Useful if gradients are lacking

Otherwise, no advantage over berny

- QST2 (uses reactant + product structures)

Order of atoms must be same in R and P

Linear interpol. in redundant internal coords.

Will not work for HCN -> HNC

See: <http://www.chemie.uni-muenchen.de/oc/zipse/lv18099/stqn.html>

- QST3 (uses reactant, product, and guess for TS)

- Path = M (optimizes discretized path)

Should specify also qst2 or qst3

Uses linear interpolation to get starting points

Might need to use guess=always

Might need to specify “BimolecularReactant”
or “BimolecularProduct”

- NEB (coded up in Jordan group)

Similar to "path"

First derivatives only

Some general comments about TS opt. and G03

QST2 - Need to merge reactant and product files, the latter starting with title, and separated by blank line

Can run G03W directly

If you are on a computer with a full install, there are examples of inputs for about 350 different types of calculations.

Find the G03w directory

Look for the “**examples**” and “**tests**” subdirectories.

tests.idx gives a short description of the various tests.