

# Lecture 6: N-grams and Conditional Probability

Ling 1330/2330 Computational Linguistics  
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# Objectives

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- ▶ Exercise #4 review
  - ◆ Unigram frequency
  - ◆ Bigram frequency
  - ◆ So many data objects!
  
- ▶ Bigrams vs. conditional probability
  
- ▶ NLTK
  - ◆ `nltk.ConditionalFreqDist`:
    - ← Conditional frequency distribution

# Exercise #4 review

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▶ <https://sites.pitt.edu/~naraehan/ling1330/ex4.html>

▶ Many different data object types!

← You must keep close tabs.

1. raw text (`str` type)
2. word tokens (`list` type)
3. word types (either `list` or `set`)
4. word frequency distribution (`nltk.FreqDist`)
  - ◆ key: word, value: frequency count
5. bigrams (*generator* type, you can cast it into a `list`)
6. bigram frequency distribution (`nltk.FreqDist`)
  - ◆ key: (w1, w2), value: frequency count

# Exercise #4

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- ▶ Pickling. What is the point?
- ▶ Shell crashing! Squeezing! Best practices?
  - ◆ Edit out big flashed chunks from your shell file before submission along with errors that aren't helpful. Your submission is also your notes for future reference!
- ▶ This way or tokenizing is not ideal. Why?
  - ◆ `etoks = nltk.word_tokenize(etxt.lower())`
- ▶ Working with complex data types (bigrams in particular)
- ▶ Membership test and data type:
  - ◆ `x in list` vs. `x in set`
  - ← One of them is much more efficient. Which?
- ▶ Surprise! Looping through (=list-comprehending) NLTK's FreqDist already follows a default order: from most frequent to least

```
>>> efreq['so']
968
>>> sograms = [gram for gram in e2gramfd if gram[0]=='so']
>>> sorted(sograms, key=e2gramfd.get, reverse=True)[:10]
[('so', 'much'), ('so', 'very'), ('so', ', '), ('so', 'well'),
 ('so', 'many'), ('so', 'long'), ('so', '.'), ('so', 'little'),
 ('so', 'far'), ('so', 'i')]
>>> for gram in sograms[:10]:
...     print(gram, e2gramfd[gram])
...
('so', 'much') 98
('so', 'very') 83
('so', ', ') 34
('so', 'well') 31
('so', 'many') 29
('so', 'long') 27
('so', '.') 21
('so', 'little') 20
('so', 'far') 19
('so', 'i') 18
>>> e2gramfd.freq(('so', 'well'))
0.00016164354990092815
```

In the latest NLTK version, sograms is already sorted by frequency!

So, sorting is not necessary. We can just use sograms[:10]

```

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>>> e2gramfd.freq(('so', 'well'))
0.00016164354990092815

```

Jane Austen just typed in 'so'.  
What is the **probability of 'well' being her next word?**

This is **conditional probability**:  
Condition: 'so'  
Outcome: 'well'

Nope, this is not it.  
(Why?)

```

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>>> sorted(sograms, key=e2gramfd.get, reverse=True)[:10]
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>>> e2gramfd.freq(('so', 'well'))
0.00016164354990092815

```

Jane Austen just typed in 'so'.  
What is the **probability of 'well' being her next word?**

This is **conditional probability**:  
Condition: 'so'  
Outcome: 'well'

**Answer:**  
 $31 / 968 = 0.032$

# nltk.ConditionalFreqDist

- Builds on FreqDist as a conditional frequency distribution.

```
>>> e2grams[-10:]  
[('fully', 'answered'), ('answered', 'in'), ('in', 'the'),  
 ('the', 'perfect'), ('perfect', 'happiness'), ('happiness',  
 'of'), ('of', 'the'), ('the', 'union'), ('union', '.'), ('.',  
 'finis')]  
  
>>> e2gramcfd = nltk.ConditionalFreqDist(e2grams)  
  
>>> e2gramcfd['so']  
FreqDist({'much': 98, 'very': 83, ',': 34, 'well': 31, 'many':  
 29, 'long': 27, '.': 21, 'little': 20, 'far': 19, 'i': 18, ...})  
  
>>> e2gramcfd['so']['well']  
31  
  
>>> e2gramcfd['so'].freq('well')  
0.03202479338842975
```

Builds from bigrams

Key: w1, Value: FreqDist of w2

Lookup w1, then w2 on returned FreqDist

Conditional probability of  
'well' following 'so'



# Bad weather vs. Pitt

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- ▶ `ConditionalFreqDist`: its keys are "conditions", and values are their respective frequency distribution `FreqDist`.
- ▶ Built from a list of **(condition, outcome)** tuples.

```
>>> school = [('rain', 'open'), ('rain', 'open'), ('rain', 'open'),
              ('rain', 'open'), ('rain', 'closed'), ('snow', 'closed'), ('snow',
              'closed'), ('snow', 'open'), ('snow', 'open'), ('snow', 'closed'),
              ('blizzard', 'closed'), ('blizzard', 'closed')]
>>> school_cfd = nltk.ConditionalFreqDist(school)
>>> school_cfd.keys()
dict_keys(['snow', 'blizzard', 'rain'])
>>> school_cfd.values()
dict_values([FreqDist({'closed': 3, 'open': 2}), FreqDist({'closed':
2}), FreqDist({'open': 4, 'closed': 1})])
>>> school_cfd.conditions()
['snow', 'blizzard', 'rain']
```

# Bad weather vs. Pitt

```
>>> school_cfd['snow']
FreqDist({'closed': 3, 'open': 2})
>>> school_cfd['snow']['closed']
3
>>> school_cfd['snow']['open']
2
>>> school_cfd['snow'].freq('open')
0.4
>>> school_cfd['blizzard']
FreqDist({'closed': 2})
>>> school_cfd['blizzard']['closed']
2
>>> school_cfd['blizzard']['open']
0
>>> school_cfd.tabulate()
          closed open
blizzard    2    0
rain        1    4
snow        3    2
>>>
```

Conditional probability  
of Pitt opening (outcome)  
when it snows (condition)

# A bit of background

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▶  **$P(A)$** : the probability of A occurring

- ◆  $P(\text{snow})$ : the probability of having a snowy weather.

▶  **$P(A | B)$** : **Conditional probability**

the probability of A occurring, given that B has occurred

- ◆  $P(\text{close} | \text{snow})$ : given a snowy weather, the probability of Pitt closing.
- ◆  $P(\text{snow} | \text{close})$ : given Pitt's closure, the probability of the day being snowy.

▶  **$P(A, B)$** : **Joint probability**

the probability of A occurring *and* B occurring

- ◆ Same as  $P(B, A)$ .
- ◆ If A and B are independent events, same as  $P(A) * P(B)$ .  
If not, same as  $P(A | B) * P(B)$  and also  $P(B | A) * P(A)$ .
- ◆  $P(\text{close, snow})$ : the probability of Pitt closing and the weather being snowy.

# bigram FD vs. CFD: very different!

```
>>> e2grams[-10:]
[('fully', 'answered'), ('answered', 'in'), ('in', 'the'), ('the',
'perfect'), ('perfect', 'happiness'), ('happiness', 'of'), ('of', 'the'),
('the', 'union'), ('union', '.'), ('.', 'finis')]

>>> e2gramfd = nltk.FreqDist(e2grams)
>>> e2gramfd[('so', 'well')]
31
>>> e2gramfd.freq(('so', 'well'))
0.0001616511359903218

>>> e2gramcfd = nltk.ConditionalFreqDist(e2grams)
>>> e2gramcfd['so']
FreqDist({'much': 98, 'very': 83, ',': 34, 'well': 31, 'many': 29, 'long':
27, '.': 21, 'little': 20, 'far': 19, 'i': 18, ...})
>>> e2gramcfd['so']['well']
31
>>> e2gramcfd['so'].freq('well')
0.03202479338842975
```

Made from the same bigrams as input, but returns different data objects

It's important you keep tabs on many data objects and their meaning!

# bigram FD vs. CFD: Practice

10 minutes



```
>>> e2grams[-10:]
[('fully', 'answered'), ('answered', 'in'), ('in', 'the'), ('the',
'perfect'), ('perfect', 'happiness'), ('happiness', 'of'), ('of', 'the'),
('the', 'union'), ('union', '.'), ('.', 'finis')]

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>>> e2gramcfd['so']['well']
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>>> e2gramcfd['so'].freq('well')
0.03202479338842975
```

Poke your object in shell to understand its structure!

10 minutes



- 
- ▶ FD vs. CFD practice
  - ▶ CFD with **trigrams!**
    - ◆ How to build?
    - ◆ What are top words following 'so well'? How about 'of the'?
  - ▶ Fun with ENABLE words
    - ◆ No vowels? Palindromes? Anagrams of 'stop'?
    - ◆ How many potential answers for Wordle?

← **Saved SHELL session posted** next to the lecture PDF!

# Where are we on the NLTK Book?

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- ▶ Ch.1 Language Processing and Python
  - ◆ <https://www.nltk.org/book/ch01.html>
  - ◆ NLTK built-in functions for exploring text, Python basics
- ▶ Ch.2 Accessing Corpora and Lexical Resources
  - ◆ <https://www.nltk.org/book/ch02.html>
  - ◆ A tour of various NLTK-loaded corpora and resources
- ▶ Ch.3 Processing Raw Text
  - ◆ <https://www.nltk.org/book/ch03.html>
  - ◆ Basic text processing pipeline – tokenization, etc.
  - ◆ Also: regular expressions

# Wrap-up

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- ▶ Homework #2 out
  - ◆ START EARLY! Get help earlier.
- ▶ Next class (Tue):
  - ◆ N-gram language models
- ▶ Review the NLTK Book, chapters 1 through 3.