

Maple commands define a function

```
> f:=x*(1-x-b*y)+y*(2-y-c*x);
```

$$f := x(1 - x - by) + y(2 - y - cx) \quad (1)$$

Take the derivatives of this wrt x and y

```
> dx:=diff(f,x);
```

$$dx := 1 - 2x - by - yc \quad (2)$$

```
> dy:=diff(f,y);
```

$$dy := -xb + 2 - 2y - cx \quad (3)$$

Solve for dx=dy=0 for (x,y) put multiple equations in {}

```
> ans:=simplify(solve({dx,dy},{x,y}));
```

$$ans := \left\{ x = \frac{2(-1+b+c)}{-4+b^2+2bc+c^2}, y = \frac{-4+c+b}{-4+b^2+2bc+c^2} \right\} \quad (4)$$

Note that simplify(stuff) and expand(stuff) can lead to more readable stuff. I will now copy the answers into new variables

```
> xs:=(2*(-1+b+c))/(-4+b^2+2*b*c+c^2);
```

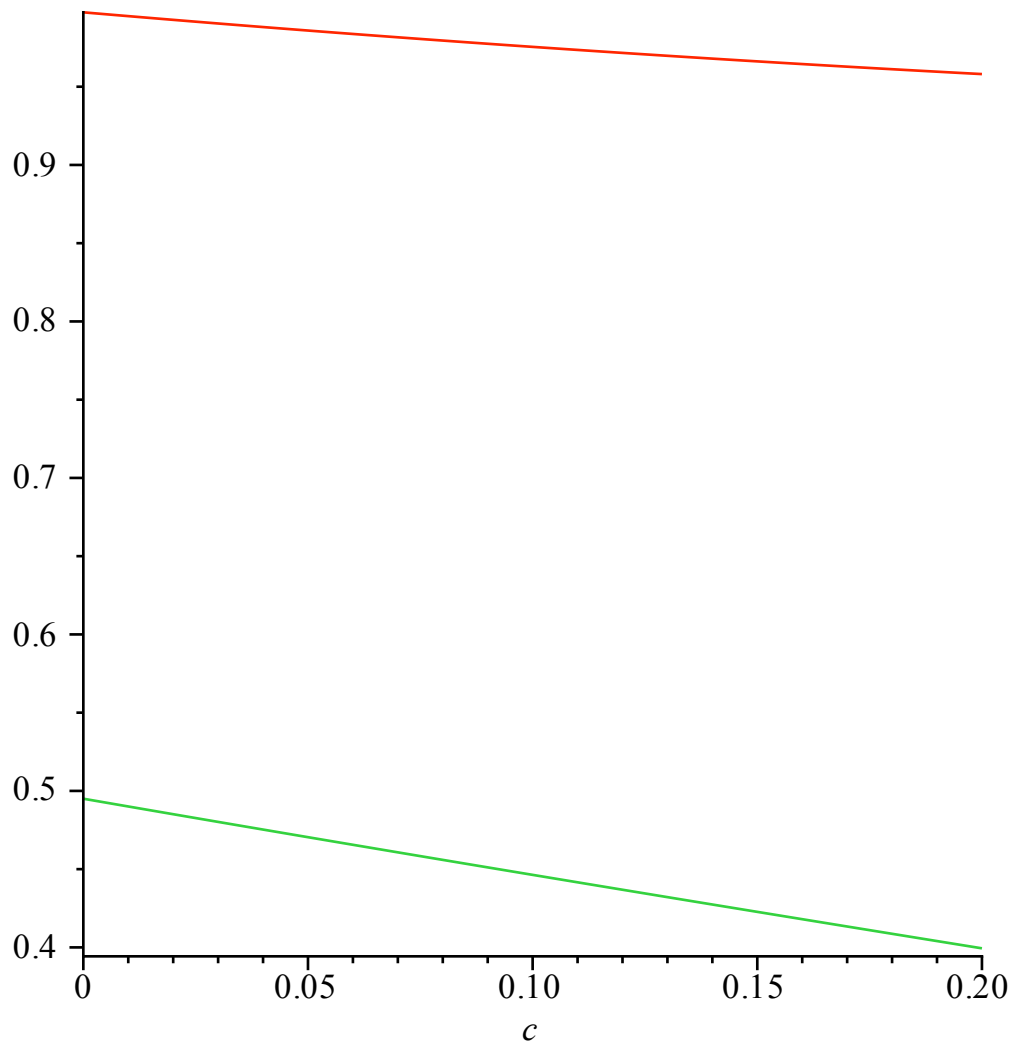
$$xs := \frac{2(-1+b+c)}{-4+b^2+2bc+c^2} \quad (5)$$

```
> ys:=(-4+c+b)/(-4+b^2+2*b*c+c^2);
```

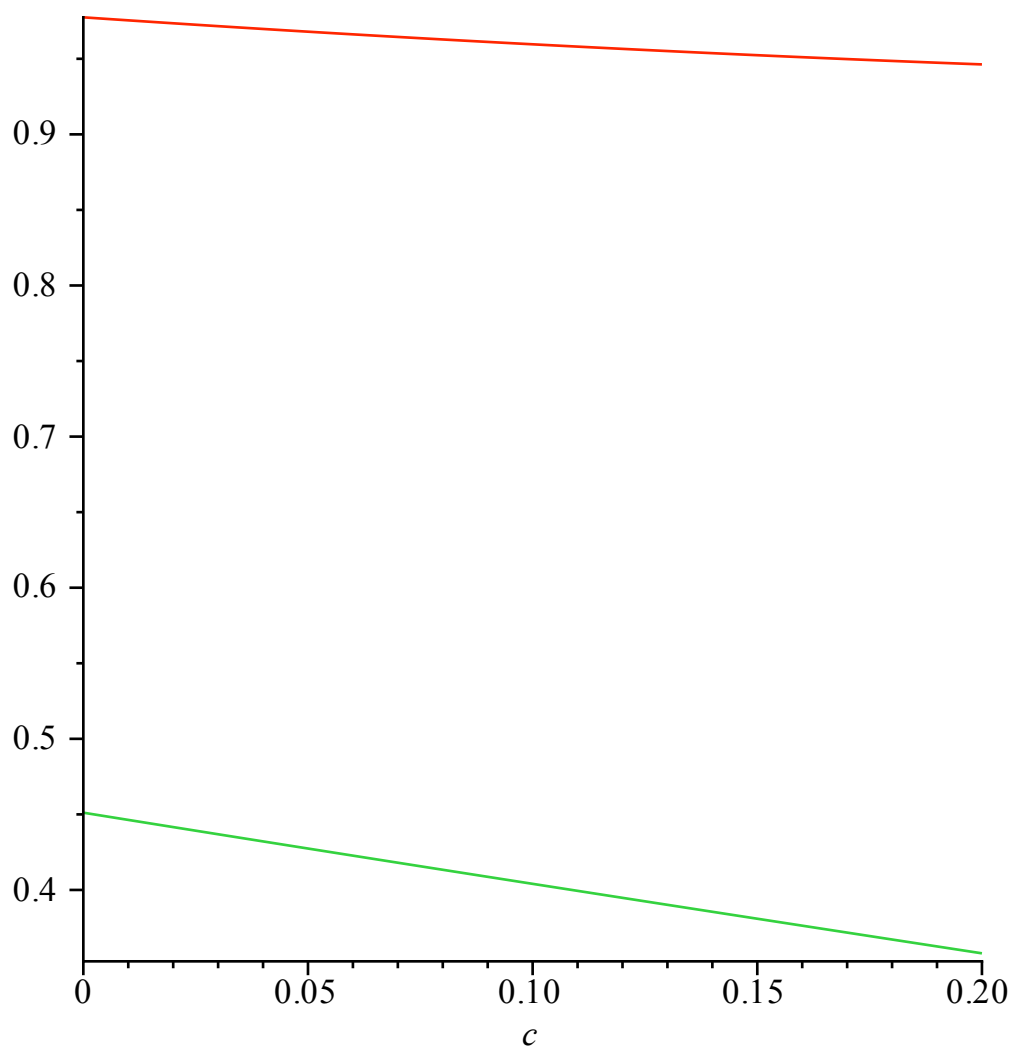
$$ys := \frac{-4+c+b}{-4+b^2+2bc+c^2} \quad (6)$$

I'll plot both of these as a function of c for b fixed using the subs command - note ys is the larger one:

```
> plot({subs(b=.01,xs),subs(b=.01,ys)},c=0..0.2);
```



```
> plot({subs(b=0.1,xs),subs(b=0.1,ys)},c=0..0.2);
```



Sensitivity of  $x_s$  to  $b$ :

> `sxb:=simplify((b/xs)*diff(xs,b));`

$$sxb := -\frac{(4 + b^2 + 2bc + c^2 - 2b - 2c)b}{(-4 + b^2 + 2bc + c^2)(-1 + b + c)} \quad (7)$$

> `sxb0:=subs(c=.25,b=.1,sxb);`

$$sxb0 := -0.1357932847 \quad (8)$$

Do an integral:

> `int(sin(2*x)*cos(x)^3,x);`

$$-\frac{1}{40} \cos(5x) - \frac{1}{4} \cos(x) - \frac{1}{8} \cos(3x) \quad (9)$$

> `int(sin(2*x)*cos(x)^3,x=0..Pi/2);`

$$\frac{2}{5} \quad (10)$$

solve a differential equation:

> `dsolve({diff(x(t),t)=x(t)*(1-x(t)/5),x(0)=1},x(t));`

$$x(t) = \frac{5}{1 + 4e^{-t}} \quad (11)$$

